

## Chapter 2: Atomic Structure

### Examples

1. Calculate the number of protons, neutrons and electrons in  ${}_{35}^{80}\text{Br}$ .

**Answer:** Here  ${}_{35}^{80}\text{Br}$  is given that where  $Z = 35$ ,  $A = 80$

i.e. species is neutral

NO. of protons = no. of electrons =  $Z = 35$

No. of neutrons =  $80 - 35 = 45$  i.e. Mass no. – No. of protons

2. The number of electrons, protons and neutrons in a species are equal to 18, 16, 16 respectively. Assign the proper symbol to the species

**Answer:** It is given that atomic number is equal to no. of protons i.e. 16 and at that it is sulphur (S)

As we know that Atomic mass = No. of protons + No. of neutrons

$$= 16 + 16 = 32$$

Here, species is not neutral because protons is not equal to electrons

Thus, it is negatively charged which is equal to excess electrons =  $18 - 16 = 2$

So, it gives us symbol  ${}_{16}^{32}\text{S}^{2-}$

3. The Vividh Bharati station of All India Radio, Delhi, broadcasts on a frequency of 1.368 kHz Calculate the wavelength of the electromagnetic radiation emitted by transmitter. Which part of the electromagnetic spectrum does it belong to?

**Answer:** Here, wave length =  $\lambda$  and it is equal to  $\frac{c}{\nu}$

i.e.  $c$  is speed of electromagnetic radiation in vacuum and  $\nu$  is the frequency

Substitute values, we get

$$\begin{aligned}
 \lambda &= \frac{c}{\nu} \\
 &= \frac{3.00 \times 10^8 \text{ ms}^{-1}}{1368 \text{ kHz}} \\
 &= \frac{3.00 \times 10^8 \text{ m s}^{-1}}{1368 \times 10^3 \text{ s}^{-1}} \\
 &= 219.3 \text{ m}
 \end{aligned}$$

Hence, It is a characteristic radiowave wave length

4. The wavelength range of the visible spectrum extends from violet (400 nm) to red (750 nm) . Express these wavelengths in frequencies (Hz)(1 nm = 10<sup>-9</sup> m) .

**Answer:** Frequency of violet line

$$\begin{aligned}
 \nu &= \frac{c}{\lambda} \\
 &= \frac{3.00 \times 10^8 \text{ ms}^{-1}}{400 \times 10^{-9} \text{ m}} \\
 &= 7.50 \times 10^{14} \text{ Hz}
 \end{aligned}$$

Frequency of red light

$$\begin{aligned}
 \nu &= \frac{c}{\lambda} \\
 &= \frac{3.00 \times 10^8 \text{ ms}^{-1}}{750 \times 10^{-9} \text{ m}} \\
 &= 4.00 \times 10^{14} \text{ Hz}
 \end{aligned}$$

Hence, range of visible spectrum is from 4.00 × 10<sup>14</sup> Hz to 7.50 × 10<sup>14</sup> Hz

5. Calculate (a) wavenumber

(b) Frequency of yellow radiation having wavelength 5800 Å

**Answer:** (a) Here, wavenumber denotes as ( $\bar{\nu}$ )

$$\begin{aligned}
 \lambda &= 5800 \text{ Å} \\
 &= 5800 \times 10^{-8} \text{ cm} = 5800 \times 10^{-10} \text{ m} \\
 \bar{\nu} &= \frac{1}{\lambda} \\
 &= \frac{1}{5800 \times 10^{-10} \text{ m}} \\
 &= 1.724 \times 10^6 \text{ m}^{-1} = 1.724 \times 10^4 \text{ cm}^{-1}
 \end{aligned}$$

(b) Here, frequency denotes as  $\nu$

$$\begin{aligned}
 \bar{\nu} &= \frac{c}{\lambda} \\
 &= \frac{3 \times 10^8 \text{ m s}^{-1}}{5800 \times 10^{-10} \text{ m}} \\
 &= 5.172 \times 10^{14} \text{ s}^{-1}
 \end{aligned}$$

6. Calculate energy of one mole of photons of radiation whose frequency is 5 × 10<sup>14</sup> Hz .

**Answer:** Given that

$$h = 6.626 \times 10^{-34} \text{ J s}$$

$$\nu = 5 \times 10^{14} \text{ s}^{-1}$$

As energy denotes by  $E$  and it is given by expression  $E = h\nu$ , So

$$\begin{aligned}
 E &= (6.626 \times 10^{-34} \text{ J s}) \times (5 \times 10^{14} \text{ s}^{-1}) \\
 &= 3.313 \times 10^{-19} \text{ J}
 \end{aligned}$$

Now, energy of one mole of photons

$$\begin{aligned}
 &= (3.313 \times 10^{-19} \text{ J}) \times (6.022 \times 10^{23} \text{ mol}^{-1}) \\
 &= 199.51 \text{ kJ mol}^{-1}
 \end{aligned}$$

**7. A 100 watt bulb emits monochromatic light of wavelength 400nm. Calculate the number of photons emitted per second by the bulb.**

**Answer:** Here, power of bulb = 100 watt =  $100 \text{ J s}^{-1}$

Energy of one photon  $E = h\nu$

$$\begin{aligned}
 &= \frac{hc}{\lambda} \\
 &= \frac{6.626 \times 10^{-34} \text{ J s} \times 3 \times 10^8 \text{ m s}^{-1}}{400 \times 10^{-9} \text{ m}} \\
 &= 4.969 \times 10^{-19} \text{ J}
 \end{aligned}$$

$$\begin{aligned}
 \text{No. of photons emitted} &= \frac{100 \text{ J s}^{-1}}{4.969 \times 10^{-19} \text{ J}} \\
 &= 2.012 \times 10^{20} \text{ s}^{-1}
 \end{aligned}$$

**8. When electromagnetic radiation of wavelength 300 nm falls on the surface of sodium, electrons are emitted with a kinetic energy of  $1.68 \times 10^5 \text{ J mol}^{-1}$ . What is the minimum energy needed to remove an electron from sodium? What is the maximum wavelength that will cause a photoelectron to be emitted?**

**Answer:** Energy ( $E$ ) of 300 nm photon given as  $h\nu = \frac{hc}{\lambda}$

$$\begin{aligned}
 &= \frac{6.626 \times 10^{-34} \text{ J s} \times 3.0 \times 10^8 \text{ m s}^{-1}}{300 \times 10^{-9} \text{ m}} \\
 &= 6.626 \times 10^{-19} \text{ J}
 \end{aligned}$$

$$\text{Energy of one mole of photons} = 6.626 \times 10^{-19} \text{ J} \times 6.022 \times 10^{23} \text{ mol}^{-1}$$

$$= 3.99 \times 10^5 \text{ J mol}^{-1}$$

So, minimum energy needed to remove one mole of electrons from sodium

$$= (3.99 - 1.68) \times 10^5 \text{ J mol}^{-1}$$

$$= 2.31 \times 10^5 \text{ J mol}^{-1}$$

Now, minimum energy for one electron

$$= \frac{2.31 \times 10^5 \text{ J mol}^{-1}}{6.022 \times 10^{23} \text{ electrons mol}^{-1}}$$

$$= 3.84 \times 10^{-19} \text{ J}$$

$$\lambda = \frac{hc}{E}$$

$$= \frac{6.626 \times 10^{-34} \text{ J s} \times 3.0 \times 10^8 \text{ m s}^{-1}}{3.84 \times 10^{-19} \text{ J}}$$

$$= 517 \text{ nm}$$

**9. The threshold frequency  $\nu_0$  for a metal is  $7.0 \times 10^{14} \text{ s}^{-1}$ . Calculate the kinetic energy of an electron emitted when radiation of frequency  $\nu = 1.0 \times 10^{15} \text{ s}^{-1}$  hits the metal.**

**Answer:** Here kinetic energy =  $\frac{1}{2} m_e v^2$

$$= h(\nu - \nu_0)$$

$$= (6.626 \times 10^{-34} \text{ J s})(1.0 \times 10^{15} \text{ s}^{-1} - 7.0 \times 10^{14} \text{ s}^{-1})$$

$$= (6.626 \times 10^{-34} \text{ J s})(10.0 \times 10^{14} \text{ s}^{-1} - 7.0 \times 10^{14} \text{ s}^{-1})$$

$$= (6.626 \times 10^{-34} \text{ J s}) \times (3.0 \times 10^{14} \text{ s}^{-1})$$

$$= 1.988 \times 10^{-19} \text{ J}$$

**10. What are the frequency and wavelength of a photon emitted during a transition from  $n=5$  state to the  $n=2$  state in the hydrogen atom.**

**Answer:** As  $n_1 = 5$ ,  $n_2 = 2$  here this transition gives rise to spectral line in the visible region. So,

$$\Delta E = 2.18 \times 10^{-18} \text{ J} \left[ \frac{1}{5^2} - \frac{1}{2^2} \right]$$

$$= -4.58 \times 10^{-19} \text{ J}$$

Thus, it's an emission energy

$$\text{Frequency of photon } \nu = \frac{\Delta E}{h}$$

$$= \frac{4.58 \times 10^{-19} \text{ J}}{6.626 \times 10^{-34} \text{ J s}}$$

$$= 6.91 \times 10^{14} \text{ Hz}$$

$$\lambda = \frac{c}{\nu}$$

$$= \frac{3.0 \times 10^8 \text{ m s}^{-1}}{6.91 \times 10^{14} \text{ Hz}}$$

$$= 434 \text{ nm}$$

**11. Calculate the energy associated with the first orbit of  $\text{He}^+$ . What is the radius of this orbit?**

**Answer:**  $E_n = -\frac{(2.18 \times 10^{-18} \text{ J})Z^2}{n^2} \text{ atom}^{-1}$

So, For  $\text{He}^+$ ,  $n = 1$ ,  $Z = 2$

i.e.  $E_1 = -\frac{(2.18 \times 10^{-18} \text{ J})(2^2)}{1^2}$

$$= -8.72 \times 10^{-18} \text{ J}$$

So, radius of orbit given as

$$r_n = \frac{(0.0529 \text{ nm})n^2}{Z}$$

As  $n = 1$ ,  $Z = 2$

$$r_n = \frac{(0.0529 \text{ nm})1^2}{2}$$

$$= 0.02645 \text{ nm}$$

**12. What will be the wavelength of a ball of mass 0.1 kg moving with a velocity of  $10 \text{ m s}^{-1}$ .**

**Answer:** According to brogile equation i.e.  $\lambda = \frac{h}{m\nu} = \frac{h}{p}$

$$\lambda = \frac{h}{m\nu}$$

$$= \frac{(6.626 \times 10^{-34} \text{ Js})}{(0.1 \text{ kg})(10 \text{ m s}^{-1})}$$

$$= 6.626 \times 10^{-34} \text{ m} \quad (\text{J} = \text{kg m}^2 \text{ s}^{-2})$$

13. The mass of an electron is  $9.1 \times 10^{-31}$  kg . If its K.E. is  $3.0 \times 10^{-25}$  J , calculate its wavelength.

**Answer:** As, K.E. =  $\frac{1}{2}mv^2$

$$\begin{aligned}
 v &= \left( \frac{2 \text{ K.E.}}{m} \right)^{\frac{1}{2}} \\
 &= \left( \frac{2 \times 3.0 \times 10^{-25} \text{ kg m}^2 \text{ s}^{-2}}{9.1 \times 10^{-31} \text{ kg}} \right)^{\frac{1}{2}} \\
 &= 812 \text{ m s}^{-1} \\
 \lambda &= \frac{h}{mv} = \frac{6.626 \times 10^{-34} \text{ Js}}{(9.1 \times 10^{-31} \text{ kg})(812 \text{ m s}^{-1})} \\
 &= 8967 \times 10^{-10} \text{ m} \\
 &= 896.7 \text{ nm}
 \end{aligned}$$

14. Calculate the mass of a photon with wavelength  $3.6 \text{ \AA}$  .

**Answer:** Here,  $\lambda = 3.6 \text{ \AA}$

$$= 3.6 \times 10^{-10} \text{ m}$$

So, velocity of photon = velocity of light

$$\begin{aligned}
 m &= \frac{h}{\lambda \nu} \\
 &= \frac{6.626 \times 10^{-34} \text{ Js}}{(3.6 \times 10^{-10} \text{ m})(3 \times 10^8 \text{ ms}^{-1})} \\
 &= 6.135 \times 10^{-29} \text{ kg}
 \end{aligned}$$

15. A microscope using suitable photons is employed to locate an electron in an atom within a distance of  $0.1 \text{ \AA}$  . What is the uncertainty involved in the measurement of its velocity?

**Answer:** As  $\Delta x \Delta p = \frac{h}{4\pi}$  or  $\Delta x m \Delta v = \frac{h}{4\pi}$

$$\Delta v = \frac{h}{4\pi \Delta x m}$$

$$\begin{aligned}
 \Delta v &= \frac{6.626 \times 10^{-34} \text{ Js}}{4 \times 3.14 \times 0.1 \times 10^{-10} \text{ m} \times 9.11 \times 10^{-31} \text{ kg}} \\
 &= 0.579 \times 10^7 \text{ m s}^{-1} \quad (1 \text{ J} = 1 \text{ kg m}^2 \text{ s}^{-2}) \\
 &= 5.79 \times 10^6 \text{ m s}^{-1}
 \end{aligned}$$

**16. A golf ball has a mass of 40 g and a speed of 45 m/s if the speed can be measured within accuracy of 2%, calculate the uncertainty in the position.**

**Answer:** As given that uncertainty in speed = 2%

$$\Rightarrow 45 \times \frac{2}{100} = 0.9 \text{ m s}^{-1}$$

$$\Rightarrow \Delta x = \frac{h}{4\pi m \Delta v}$$

$$= \frac{6.626 \times 10^{-34} \text{ Js}}{4 \times 3.14 \times 40 \text{ g} \times 10^{-3} \text{ kg g}^{-1} (0.9 \text{ m s}^{-1})}$$

$$= 1.46 \times 10^{-33} \text{ m}$$

Approximately it is near to  $10^{18}$  times smaller than the diameter of typical atomic nucleus.

**17. What is the total number of orbitals associated with the principle quantum number n=3.**

**Answer:** As it is given that  $n = 3$

So, possible values for  $l = 0, 1, 2$

Hence, there is 1 3s orbital i.e.  $n = 3, l = 1, m_l = 0$

And there are 3 3p orbitals i.e.  $n = 3, l = 1, m_l = -1, 0, +1$

And there are 5 3d orbitals i.e.  $n = 3, l = 2, m_l = -2, -1, 0, +1, +2$

So, total orbitals =  $1+3+5 = 9$

No. of orbitals =  $n^2 = 3^2 = 9$

**18. Using s, p, d, f notations, describe the orbital with the following quantum numbers**

- (a)  $n = 2, l = 1$
- (b)  $n = 4, l = 0$
- (c)  $n = 5, l = 3$
- (d)  $n = 3, l = 2$

**Answer:** Here, orbitals are

- (a)  $n = 2, l = 1$ , orbital = 2p
- (b)  $n = 4, l = 0$ , orbital = 4s
- (c)  $n = 5, l = 3$ , orbital = 5f
- (d)  $n = 3, l = 2$ , orbital = 3d

### Exercise

1. (i) Calculate the number of electrons which will together weigh one gram
- (ii) Calculate the mass and charge of one mole of electrons

**Answer:** (i) Here mass of one electron =  $9.10939 \times 10^{-31}$  kg

No. of electrons weigh =  $9.10939 \times 10^{-31}$  kg = 1

No. of electrons will weigh = 1 g ( $1 \times 10^{-3}$  kg)

$$\begin{aligned}
 &= \frac{1}{9.10939 \times 10^{-31} \text{ kg}} \times (1 \times 10^{-3} \text{ kg}) \\
 &= 0.1098 \times 10^{-3+31} \\
 &= 0.1098 \times 10^{28} \\
 &= 1.098 \times 10^{27}
 \end{aligned}$$

(ii) As mass of one electron =  $9.10939 \times 10^{-31}$  kg

Mass of one mole of electron =  $(6.022 \times 10^{23}) \times (9.10939 \times 10^{-31} \text{ kg}) = 5.48 \times 10^{-7}$  kg

Charge on one electron =  $1.6022 \times 10^{-19}$  coulomb

Charge on one mole of electron =  $(1.6022 \times 10^{-19} \text{ C}) (6.022 \times 10^{23}) = 9.65 \times 10^4 \text{ C}$

2. (i) Calculate the total number of electrons present in one mole of methane.

(ii) Find (a) the total number and (b) the total mass of neutrons in 7mg of  $^{14}\text{C}$

(Assume that mass of a neutron =  $1.675 \times 10^{-27}$  kg).



(iii) Find (a) the total number and (b) the total mass of protons in 34 mg of  $\text{NH}_3$  at STP. Will the answer change if the temperature and pressure are changed?

**Answer:** (i) Methane represents as  $\text{CH}_4$

$$\begin{aligned}
 \text{No. of electrons in one mole molecules of methane} &= 6.023 \times 10^{23} \\
 &= 6.022 \times 10^{23} \times 10 \\
 &= 6.022 \times 10^{24}
 \end{aligned}$$

(ii) (a) As no. of atoms in one mole =  $6.023 \times 10^{23}$

As one atom of  $^{14}\text{C}$  have eight neutrons

So, no. of neutrons in 14 g of  $^{14}\text{C}$  =  $(6.023 \times 10^{23}) \times 8$  or  $(6.022 \times 10^{23} \times 8)$  neutrons

$$\text{Thus, No. of neutrons in 7 mg} = \frac{6.022 \times 10^{23} \times 8 \times 7 \text{mg}}{1400 \text{mg}} = 2.4092 \times 10^{21}$$

(b) Mass of one neutron =  $1.67493 \times 10^{-27}$  kg

So, mass of total neutrons in 7 g of  $^{14}\text{C}$

$$\begin{aligned}
 &= (2.4092 \times 10^{21})(1.67493 \times 10^{-27} \text{ kg}) \\
 &= 4.0352 \times 10^{-6} \text{ kg}
 \end{aligned}$$

(iii) (a) One mole of  $\text{NH}_3$  =  $\{1(14)+3(1)\}$ g of  $\text{NH}_3$  = 17 g of  $\text{NH}_3$

$$= 6.022 \times 10^{23} \text{ molecules of } \text{NH}_3$$

Total protons in one molecule of  $\text{NH}_3$  =  $\{1(7)+3(1)\}$  = 10

No. of protons in  $6.023 \times 10^{23}$  molecules of  $\text{NH}_3$

$$\begin{aligned}
 &= (6.023 \times 10^{23})(10) \\
 &= 6.023 \times 10^{24}
 \end{aligned}$$

This implies 17 g of  $\text{NH}_3$  have  $(6.023 \times 10^{24})$  protons

No. of protons in 34 mg of  $\text{NH}_3$

$$= \frac{6.022 \times 10^{24} \times 34 \text{ mg}}{17000 \text{ mg}} = 1.2046 \times 10^{22}$$

(b) Mass of one proton =  $1.67493 \times 10^{-27}$  kg

So, Total mass of proton in 34 mg of  $\text{NH}_3$

$$= (1.67493 \times 10^{-27} \text{ kg})(1.2046 \times 10^{22})$$

$$= 2.0176 \times 10^{-5} \text{ kg}$$

Thus, values remain unchanged if temperature and pressure changed because protons, electrons, neutrons is independent of temperature and pressure.

### 3. How many neutrons and protons are there in the following nuclei?



**Answer:**  ${}_{6}^{13}\text{C}$

Here, atomic mass = 13

Atomic number = no. of protons = 6

No. of neutrons = Atomic mass – atomic no. =  $13 - 6 = 7$



Here, atomic mass = 16

Atomic number = no. of protons = 8

No. of neutrons = Atomic mass – atomic no. =  $16 - 8 = 8$



Here, atomic mass = 24

Atomic number = no. of protons = 12

No. of neutrons = Atomic mass – atomic no. =  $24 - 12 = 12$



Here, atomic mass = 56

Atomic number = no. of protons = 26

No. of neutrons = Atomic mass – atomic no. =  $56 - 26 = 30$



Here, atomic mass = 88

Atomic number = no. of protons = 38

No. of neutrons = Atomic mass – atomic no. = 88-38 = 50

**4. Write the complete symbol for the atom with the given atomic number (Z) and Atomic mass (A)**

(i) Z = 17, A = 35

(ii) Z = 92, A = 233

(iii) Z = 4, A = 9

**Answer:** (i)  ${}_{17}^{35}\text{Cl}$

(ii)  ${}_{92}^{233}\text{U}$

(iii)  ${}_4^9\text{Be}$

**5. Yellow light emitted from a solution lamp has a wavelength  $\lambda$  of 580 nm Calculate frequency  $\nu$  and wave number  $\bar{\nu}$  of the yellow light.**

**Answer:** We have given that frequency  $\nu$  and wave number  $\bar{\nu}$  of the yellow light and  $c$  be the velocity of light =  $3 \times 10^8 \text{ m/s}$

$\lambda$  be the wavelength = 580 nm =  $580 \times 10^{-9} \text{ m}$

As we know that  $\lambda = \frac{c}{\nu}$

$$\text{So, } \nu = \frac{3 \times 10^8}{580 \times 10^{-9}} = 5.17 \times 10^{14} \text{ s}^{-1}$$

Frequency of yellow light emitted =  $5.17 \times 10^{14} \text{ s}^{-1}$

$$\text{Wave number} = \bar{\nu} = \frac{1}{\lambda}$$

$$\begin{aligned}
 &= \frac{1}{580 \times 10^{-9}} \\
 &= 1.72 \times 10^6 \text{ m}^{-1}
 \end{aligned}$$

**6. Find energy of each of the photons which**

**(i) correspond to light of frequency  $3 \times 10^{15} \text{ Hz}$**

(ii) have wave length of  $0.50\text{\AA}$

**Answer:** (i) Energy denotes as E

$$\text{So, } E = hv \quad (\text{i})$$

Here, h = planck constant =  $6.626 \times 10^{-34} \text{ Js}$

$$v = \text{frequency of light} = 3 \times 10^{15} \text{ Hz}$$

Substitute values in (i) we get

$$E = (6.626 \times 10^{-34})(3 \times 10^{15})$$

$$E = 1.988 \times 10^{-18} \text{ J}$$

(ii) Energy denotes as E and wavelength as  $\lambda$

$$\text{So, } E = \frac{hc}{\lambda} \quad (\text{i})$$

Here, h = planck constant =  $6.626 \times 10^{-34} \text{ Js}$

$$c = \text{frequency of light} = 3 \times 10^8 \text{ m/s}$$

Substitute values in (i) we get

$$E = \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{0.50 \times 10^{-10}}$$

$$E = 3.976 \times 10^{-15} \text{ J}$$

**7. Calculate the wavelength, frequency and wave number of a light wave whose period is  $2.0 \times 10^{-10} \text{ s}$ .**

**Answer:** Here frequency =  $v$ , wavelength =  $\lambda$ , Velocity of light =  $c$

$$v = \frac{1}{\text{period}} = \frac{1}{2.0 \times 10^{-10} \text{ s}} = 5.0 \times 10^9 \text{ s}^{-1}$$

$$\lambda = \frac{c}{v} \text{ where } c = 3 \times 10^8 \text{ m/s}$$

$$\Rightarrow \lambda = \frac{3 \times 10^8}{5.0 \times 10^9} = 6.0 \times 10^{-2} \text{ m}$$

$$\text{Wave number of light} = \frac{1}{\lambda} = \frac{1}{6.0 \times 10^{-2}} = 1.66 \times 10^1 \text{ m}^{-1} = 16.66 \text{ m}^{-1}$$

**8. What is the number of photons of light with a wavelength of 4000 pm that provide 1 J of energy.**

**Answer:** Here, energy  $E$  of a photon =  $h\nu$

And energy ( $E_n$ ) of  $n$  photons =  $n h\nu$

It is given that

Wavelength =  $\lambda = 4000 \text{ pm} = 4000 \times 10^{-12} \text{ m}$

Velocity =  $c = 3 \times 10^8 \text{ m/s}$

Planck constant =  $h = 6.626 \times 10^{-34} \text{ Js}$

This implies  $n = \frac{E_n \lambda}{hc}$

Substitute values in above equation, we get

$$\begin{aligned}
 n &= \frac{(1) \times (4000 \times 10^{-12})}{(6.626 \times 10^{-34})(3 \times 10^8)} \\
 &= 2.012 \times 10^{16}
 \end{aligned}$$

Thus, no. of photons =  $2.012 \times 10^{16}$

**9. A photon of wavelength  $4 \times 10^{-7} \text{ m}$  strikes on metal surface, the work function of the metal being 2.13 eV. Calculate**

**(i) the energy of the photon (eV)**

**(ii) the kinetic energy of the emission, and**

**(iii) the velocity of the photoelectron ( $1 \text{ eV} = 1.6020 \times 10^{-19} \text{ J}$ )**

**Answer:** (i) Here,

Planck constant =  $h = 6.626 \times 10^{-34} \text{ Js}$

Velocity of light =  $c = 3 \times 10^8 \text{ m/s}$

Wavelength =  $\lambda = 4 \times 10^{-7} \text{ m}$

So, energy ( $E$ ) =  $\frac{hc}{\lambda}$

Substitute values in above equation, we get

$$\begin{aligned}
 E &= \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{4 \times 10^{-7}} \\
 &= 4.9695 \times 10^{-19} \text{ J}
 \end{aligned}$$

(ii) Kinetic energy of emission denotes as  $E_k$

$$\begin{aligned}
 \text{So, } E_k &= hv - hv_0 \\
 &= (E - W) \text{ eV} \\
 &= \left( \frac{4.9695 \times 10^{-19}}{1.6020 \times 10^{-19}} \right) \text{ eV} - 2.13 \text{ eV} \\
 &= (3.1020 - 2.13) \text{ eV} \\
 &= 0.9720 \text{ eV}
 \end{aligned}$$

(iii) Here, velocity of photo electron denoted by  $v$

Ans it is calculated by using formula i.e.

$$\begin{aligned}
 \frac{1}{2} mv^2 &= hv - hv_0 \\
 v &= \sqrt{\frac{2(hv - hv_0)}{m}}
 \end{aligned}$$

Where  $(hv - hv_0)$  be kinetic energy and  $m$  be the mass

Now, substitute the values we get:

$$\begin{aligned}
 v &= \sqrt{\frac{2 \times (0.9720 \times 1.6020 \times 10^{-19}) \text{ J}}{9.10939 \times 10^{-31} \text{ kg}}} \\
 &= \sqrt{0.3418 \times 10^{12} \text{ m}^2 \text{ s}^{-2}} \\
 v &= 5.84 \times 10^5 \text{ ms}^{-1}
 \end{aligned}$$

**10. Electromagnetic radiation of wavelength 242 nm is just sufficient to ionise the sodium atom. Calculate the ionisation energy of sodium is  $\text{kJmol}^{-1}$ .**

**Answer:** Energy of sodium (E) =  $\frac{N_A hc}{\lambda}$

$$\begin{aligned}
 &= \frac{(6.023 \times 10^{23} \text{ mol}^{-1})(6.626 \times 10^{-34} \text{ J s})(3 \times 10^8 \text{ ms}^{-1})}{242 \times 10^{-9} \text{ m}} \\
 &= 4.947 \times 10^5 \text{ J mol}^{-1} \\
 &= 494.7 \times 10^3 \text{ J mol}^{-1} \\
 &= 494 \text{ kJ mol}^{-1}
 \end{aligned}$$

**11. A 25 watt bulb emits monochromatic yellow light of wavelength of  $0.57 \mu\text{m}$  . Calculate the rate of emission of quanta per second.**

**Answer:** Here P denotes power of bulb which is 25 Watt =  $25 \text{ Js}^{-1}$

And energy of one photon (E) =  $h\nu = \frac{hc}{\lambda}$

Substitute values in above equation, we get

$$\begin{aligned}
 E &= \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{(0.57 \times 10^{-6})} \\
 &= 34.87 \times 10^{-20} \text{ J}
 \end{aligned}$$

So, Rate of emission per second =  $\frac{25}{34.87 \times 10^{-20}} = 7.169 \times 10^{19} \text{ s}^{-1}$

**12. Electrons are emitted with zero velocity from a metal surface when it is exposed to radiation of wavelength  $6800 \text{ \AA}$  Calculate threshold frequency ( $\nu_0$ ) and work function  $W_0$  of the metal.**

**Answer:** Given that threshold wavelength ( $\lambda_0$ ) =  $6800 \text{ \AA} = 6800 \times 10^{-10} \text{ m}$

And threshold frequency ( $\nu_0$ ) =  $\frac{c}{\lambda_0} = \frac{3 \times 10^8 \text{ ms}^{-1}}{6.8 \times 10^{-7} \text{ m}} = 4.41 \times 10^{14} \text{ s}^{-1}$

Thus, work function ( $W_0$ ) =  $h\nu_0$

$$\begin{aligned}
 &= (6.626 \times 10^{-34} \text{ J s})(4.41 \times 10^{14} \text{ s}^{-1}) \\
 &= 2.922 \times 10^{-19} \text{ J}
 \end{aligned}$$

**13. What is the wavelength of light emitted when the electron in a hydrogen atom undergoes transition from an energy level with  $n=4$  to an energy level with  $n=2$ .**

**Answer:** Let from given condition  $n_i = 4$  to  $n_f = 2$  transition which give rise to spectral line

$$\begin{aligned}
 \text{So, energy } E &= 2.18 \times 10^{-18} \left[ \frac{1}{n_i^2} - \frac{1}{n_f^2} \right] \\
 &= 2.18 \times 10^{-18} \left[ \frac{1}{4^2} - \frac{1}{2^2} \right] \\
 &= 2.18 \times 10^{-18} \left[ \frac{1-4}{16} \right] \\
 &= 2.18 \times 10^{-18} \times \left( -\frac{3}{16} \right) \\
 &= -(4.0875 \times 10^{-19} \text{ J}) \text{ which indicates energy of emission}
 \end{aligned}$$

$$\text{So, wavelength } (\lambda) = \frac{hc}{E}$$

$$\lambda = \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{4.0875 \times 10^{-19}}$$

$$\lambda = 4.8631 \times 10^{-7} \text{ m}$$

$$= 486.3 \times 10^{-9} \text{ m}$$

$$= 486 \text{ nm}$$

**14. How much energy is required to ionise a H atom if the electron occupies n=5 orbit? Compare your answer with the ionization enthalpy of H atom (energy required to remove the electron from n=1).**

**Answer:** Energy  $E_n = \frac{-(2.18 \times 10^{-18}) Z^2}{n^2}$

where  $Z$  = atomic number

$n$  = principal quantum no.

So, for  $n_1 = 5$  to  $n_2 = \infty$

$$\Delta E = E_\infty - E_5$$

$$= \left[ \left\{ \frac{-(2.18 \times 10^{-18} \text{ J})(1)^2}{(\infty)^2} \right\} - \left\{ \frac{-(2.18 \times 10^{-18} \text{ J})(1)^2}{(5)^2} \right\} \right]$$

$$= (2.18 \times 10^{-18} \text{ J}) \left( \frac{1}{(5)^2} \right) \quad \left[ \because \frac{1}{\infty} = 0 \right]$$

$$= 0.0872 \times 10^{-18} \text{ J}$$

$$\Delta E = 8.72 \times 10^{-20} \text{ J}$$



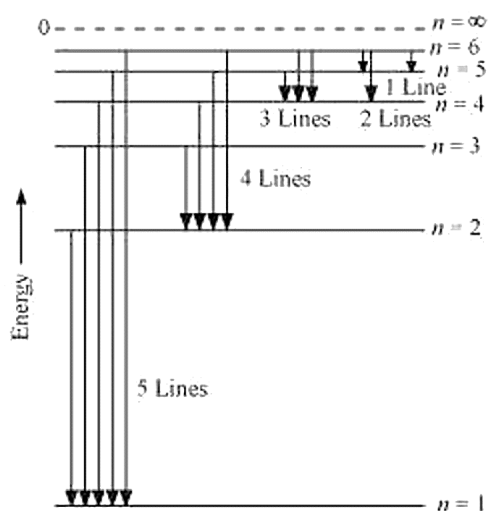
Now, energy required for  $[n_1 = 1 \text{ to } n = \infty] = 8.72 \times 10^{-20} \text{ J}$

$$\begin{aligned}
 \Delta E &= E_{\infty} - E_1 \\
 &= \left[ \left\{ \frac{-(2.18 \times 10^{-18})(1)^2}{(\infty)^2} \right\} - \left\{ \frac{-(2.18 \times 10^{-18})(1)^2}{(1)^2} \right\} \right] \\
 &= (2.18 \times 10^{-18})[1-0] \\
 &= 2.18 \times 10^{-18} \text{ J}
 \end{aligned}$$

Thus, less energy required in fifth orbital as compared to ground state.

**15. What is the maximum number of emission lines when the excited electron of an H atom in  $n=6$  drops to the ground state.**

**Answer:**



Thus, total lines in emission spectrum =  $5+4+3+2+1 = 15$

$$\text{No. of spectral lines in } n^{\text{th}} \text{ level to ground state} = \frac{n(n-1)}{2}$$

As given that  $n = 6$

$$\text{So, no. of spectral lines} = \frac{6(6-1)}{2} = 15$$

**16. (i) The energy associated with the first orbit in the hydrogen atom is  $-2.18 \times 10^{-18} \text{ J atom}^{-1}$ . What is the energy associated with the fifth orbit?**

**(ii) Calculate the radius of Bohr's fifth orbit for hydrogen atom.**

**Answer:** (i) Energy associated with the fifth orbit is

$$E_5 = \frac{-(2.18 \times 10^{-18})}{(5)^2}$$

$$= \frac{-2.18 \times 10^{-18}}{25}$$

$$E_5 = -8.72 \times 10^{-20} \text{ J}$$

(ii) Radius of Bohr  $n^{\text{th}}$  orbit ( $r_n$ ) =  $(0.0529 \text{ nm})n^2$

So, for given  $n = 5$

$$r_5 = (0.0529 \text{ nm})(5)^2$$

$$r_5 = 1.3225 \text{ nm}$$

**17. Calculate the wave number for the longest wavelength transition in the Balmer series of atomic hydrogen.**

**Answer:** As for Balmer series  $n_i = 2$

$$\text{Wave number } (\bar{\nu}) = \left[ \frac{1}{(2)^2} - \frac{1}{n_f^2} \right] (1.097 \times 10^7 \text{ m}^{-1})$$

Wave no. is inversely proportional to wave length

Thus, for longest wavelength  $\bar{\nu}$  is to be smallest

So, for  $\bar{\nu}$  to be minimum,  $n_f$  should be minimum

Thus, for balmer series, transition from  $n_i = 2$  to  $n_f = 3$  is allowed

Let  $n_f = 3$ , we get:

$$\bar{\nu} = (1.097 \times 10^7) \left[ \frac{1}{2^2} - \frac{1}{3^2} \right]$$

$$\bar{\nu} = (1.097 \times 10^7) \left[ \frac{1}{4} - \frac{1}{9} \right]$$

$$= (1.097 \times 10^7) \left( \frac{9-4}{36} \right)$$

$$= (1.097 \times 10^7) \left( \frac{5}{36} \right)$$

$$\bar{\nu} = 1.5236 \times 10^6 \text{ m}^{-1}$$

18. What is the energy in joules, required to shift the electron of the hydrogen atom from the first Bohr orbit to the fifth Bohr orbit and what is the wavelength of the light emitted when the electron returns to the ground state? The ground state electron energy is  $-2.18 \times 10^{-18}$  ergs.

**Answer:** Here, energy for bohr orbit  $E_n = \frac{-(2.18 \times 10^{-18})Z^2}{n^2}$

where  $Z$  = atomic no.

and ground state energy =  $-2.18 \times 10^{-18}$  ergs

$$= -2.18 \times 10^{-18} \times 10^{-7} \text{ J}$$

$$= -2.18 \times 10^{-18} \text{ J}$$

So, energy required to shift electron from  $n = 1$  to  $n = 5$  is

$$\Delta E = E_5 - E_1$$

$$= \frac{-(2.18 \times 10^{-18})(1)^2}{(5)^2} - (-2.18 \times 10^{-18})$$

$$= (2.18 \times 10^{-18}) \left[ 1 - \frac{1}{25} \right]$$

$$= (2.18 \times 10^{-18}) \left( \frac{24}{25} \right)$$

$$= 2.0928 \times 10^{-18} \text{ J}$$

Wavelength of emitted light =  $\frac{hc}{E}$

$$= \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{(2.0928 \times 10^{-18})}$$

$$= 9.498 \times 10^{-8} \text{ m}$$

19. The electron energy in hydrogen atom is given by  $E_n = \frac{(-2.18 \times 10^{-18})}{n^2}$  J Calculate the energy required to remove an electron completely from the  $n=2$  orbit. What is the longest wavelength of light in cm that can be used to cause this transition?

**Answer:** We have given that  $E_n = -\frac{2.18 \times 10^{-18}}{n^2}$  J

So, energy required from  $n = 2$  is  $\Delta E = E_\infty - E_2$

$$\begin{aligned}
 &= \left[ \left( \frac{-2.18 \times 10^{-18}}{(\infty)^2} \right) - \left( \frac{-2.18 \times 10^{-18}}{(2)^2} \right) \right] \text{J} \\
 &= \left[ \frac{2.18 \times 10^{-18}}{4} - 0 \right] \text{J} \\
 &= 0.545 \times 10^{-18} \text{ J} \\
 &= 5.45 \times 10^{-19} \text{ J}
 \end{aligned}$$

$$\lambda = \frac{hc}{\Delta E} \text{ where } \lambda \text{ is longest wavelength}$$

$$\begin{aligned}
 \lambda &= \frac{(6.626 \times 10^{-34})(3 \times 10^8)}{5.45 \times 10^{-19}} \\
 &= 3.647 \times 10^{-7} \text{ m} \\
 &= 3647 \times 10^{-10} \text{ m} \\
 &= 3647 \text{ \AA}
 \end{aligned}$$

**20. Calculate the wavelength of an electron moving with a velocity of  $2.05 \times 10^7 \text{ ms}^{-1}$ .**

**Answer:** As we know that by Broglie's equation  $\lambda = \frac{h}{mv}$

where  $\lambda$  = wavelength,  $m$  = mass,  $v$  = velocity,  $h$  = planck constant

Now, substituting all values

$$\begin{aligned}
 \lambda &= \frac{6.626 \times 10^{-34} \text{ Js}}{(9.10939 \times 10^{-31} \text{ kg})(2.05 \times 10^7 \text{ ms}^{-1})} \\
 \lambda &= 3.548 \times 10^{-11} \text{ m}
 \end{aligned}$$

**21. The mass of an electron is  $9.1 \times 10^{-31} \text{ kg}$  If its K.E. is  $3.0 \times 10^{-25} \text{ J}$  Calculate its wavelength.**

**Answer:** According to Broglie's equation  $\lambda = \frac{h}{mv}$  (i)

As we have kinetic energy (K.E.) =  $3.0 \times 10^{-25} \text{ J}$

As we know that  $\text{K.E.} = \frac{1}{2} mv^2$

$$\text{So, velocity (v)} = \sqrt{\frac{2 \text{ K.E.}}{m}}$$

$$\begin{aligned}
 &= \sqrt{\frac{2(3.0 \times 10^{-25} \text{ J})}{9.10939 \times 10^{-31} \text{ kg}}} \\
 &= \sqrt{6.5866 \times 10^4} \text{ v} \\
 &= 811.579 \text{ ms}^{-1}
 \end{aligned}$$

Put values in (i) we get

$$\lambda = \frac{6.626 \times 10^{-34} \text{ Js}}{(9.10939 \times 10^{-31} \text{ kg})(811.579 \text{ ms}^{-1})}$$

$$\lambda = 8.9625 \times 10^{-7} \text{ m}$$

**22. Which of the following are isoelectronic species i.e., those having the same number of electrons?**



**Answer:** Total number of electrons in Na, K, Ca, S and Ar are 11, 19, 20, 16 and 18.

Now, the number of electron in given species are,

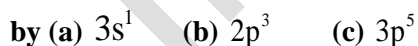
Species	Electrons
$\text{Na}^+$	$11-1=10$
$\text{K}^+$	$19-1=18$
$\text{Ca}^{2+}$	$20-2=18$
$\text{S}^{2-}$	$16+2=18$
Ar	18

So,  $\text{K}^+, \text{Ca}^{2+}, \text{S}^{2-}, \text{Ar}$  are isoelectronic species.

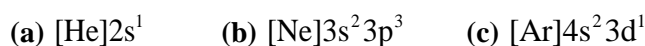
**23. (i) Write the electronic configurations of the following ions:**



**(ii) What are the atomic numbers of elements whose outermost electrons are represented?**



**(iii) Which atoms are indicated by the following configurations?**



**Answer:** (i) (a)



Here, electronic configuration of H atom =  $1s^1$

Negative charge indicates gain of an electron

So, electronic configuration of  $\text{H}^- = 1s^2$

(i) (b)

$\text{Na}^+$  ion

Here, electronic configuration of Na atom =  $1s^2 2s^2 2p^6 3s^1$

Positive charge indicates loss of an electron

So, electronic configuration of  $\text{Na}^+ = 1s^2 2s^2 2p^6 3s^0$  or  $1s^2 2s^2 2p^6$

(i) (c)

$\text{O}^{2-}$  ion

Here, electronic configuration of O atom =  $1s^2 2s^2 2p^4$

Negative charge indicates gain of two electron

So, electronic configuration of  $\text{O}^{2-} = 1s^2 2s^2 2p^6$

(i) (d)

$\text{F}^-$  ion

Here, electronic configuration of F atom =  $1s^2 2s^2 2p^5$

Negative charge indicates gain of an electron

So, electronic configuration of  $\text{F}^- = 1s^2 2s^2 2p^6$

(ii) (a)

Completing electronic configuration of element  $1s^2 2s^2 2p^6 3s^1$

No. of electrons present in atom =  $2+2+6+1 = 11$

Atomic no. = 11

(ii) (b)

Completing electronic configuration of element  $1s^2 2s^2 2p^3$

No. of electrons present in atom =  $2+2+3 = 7$

Atomic no. = 7

(ii) (c)

Completing electronic configuration of element  $1s^2 2s^2 2p^5$

No. of electrons present in atom =  $2+2+5 = 9$

Atomic no. = 9

(iii) (a)

Electronic configuration  $[\text{He}] 2s^1 = 1s^2 2s^1$

Atomic no. = 3

Thus, element with the electronic configuration  $[\text{He}] 2s^1 =$  lithium (Li)

(iii) (b)

Electronic configuration  $[\text{Ne}] 3s^2 3p^3 = 1s^2 2s^2 2p^6 3s^2 3p^3$

Atomic no. = 15

Thus, element with the electronic configuration  $[\text{Ne}] 3s^2 3p^3 =$  phosphorus (P)

(iii) (c)

Electronic configuration  $[\text{Ar}] 4s^2 3d^1 = 1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^1$

Atomic no. = 21

Thus, element with the electronic configuration  $[\text{Ar}] 4s^2 3d^1 =$  scandium (Sc)

**24. What is the lowest value of  $n$  that allows  $g$  orbitals to exist.**

**Answer:** Here, for  $g$  orbitals  $l = 4$

Since for any value of  $n$  of principal quantum no.

Azimuthal quantum no. ( $l$ ) have the value from 0 to  $(n-1)$

So, for  $l = 4$ , minimum value of  $n = 5$

**25. An electron is in one of the  $3d$  orbitals. Give the possible values of  $n, l, m_l$  for this electron.**

**Answer:** Here, for 3d orbital

Principal quantum no. (n) = 3

Azimuthal quantum no. (l) = 2

Magnetic quantum no. ( $m_l$ ) = -2, -1, 0, 1, 2

**26. An atom of an element contains 29 electrons and 35 neutrons. Deduce**

**(i) the number of protons and**

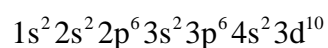
**(ii) the electronic configuration of the element.**

**Answer:** (i) Atom have to be neutral

So, no. of protons = no. of electrons

Thus, no. of protons = 29

(ii) Electronic configuration of the element is



**27. Give the number of electrons in the species  $H_2^+$ ,  $H_2$ ,  $O_2^+$**

**Answer:**  $H_2^+$

No. of electrons in  $H_2 = 1+1 = 2$

No. of electrons in  $H_2^+ = 2-1 = 1$

$H_2$

No. of electrons in  $H_2 = 1+1 = 2$

$O_2^+$

No. of electrons in  $O_2 = 8+8 = 16$

No. of electrons in  $O_2^+ = 16-1 = 15$

**28. (i) An atomic orbital has n=3 What are the possible values of l,  $m_l$**

**(ii) List the quantum numbers ( l,  $m_l$  ) of electrons for 3d orbital.**



(iii) Which of the following orbitals are possible? 1p, 2s, 2p, 3f.

**Answer:** (i) As it is given that  $n = 3$

For  $n$ ,  $l$  have values from 0 to  $(n-1)$

So, for  $n = 3$ ,  $l = 0, 1, 2$

For  $l$ ,  $m_l$  have  $(2l+1)$  values

For  $l = 0$ ,  $m = 0$ ;  $l = 1$ ,  $m = -1, 0, 1$ ;  $l = 2$ ,  $m = -2, -1, 0, 1, 2$

For  $n = 3$ ,  $l = 0, 1, 2$ ,  $m_0 = 0$ ,  $m_1 = -1, 0, 1$ ,  $m_2 = -2, -1, 0, 1, 2$

(ii) For 3d orbital  $l = 2$

For  $l$ ,  $m_l$  have  $(2l+1)$  values which is 5

For  $l = 2$ ,  $m_2 = -2, -1, 0, 1, 2$

(iii) Here from given orbitals only 2s, 2p are possible

1p, 3f can't exist

For p orbitals,  $l = 1$

For  $n$ ,  $l$  have values from zero to  $(n-1)$

For  $l = 1$ , minimum value of  $n = 2$

Now, for f orbital,  $l = 3$

For  $l = 3$  minimum value of  $n = 4$

Thus, 1p, 3f don't exist

**29. Using s, p, d notations, describe the orbital with the following quantum numbers**

(a)  $n = 1, l = 0$  (b)  $n = 3, l = 1$  (c)  $n = 4, l = 2$  (d)  $n = 4, l = 3$

**Answer:**

(a) Here orbital is 1s

(b) Here orbital is 3p

(c) Here orbital is 4d

(d) Here orbital is 4f

**30. Explain, giving reasons, which of the following sets of quantum numbers are not possible**

(a)  $n = 0, l = 0, m_l = 0, m_s = +\frac{1}{2}$

(b)  $n = 1, l = 0, m_l = 0, m_s = -\frac{1}{2}$

(c)  $n = 1, l = 1, m_l = 0, m_s = +\frac{1}{2}$

(d)  $n = 2, l = 1, m_l = 0, m_s = -\frac{1}{2}$

(e)  $n = 3, l = 3, m_l = -3, m_s = +\frac{1}{2}$

(f)  $n = 3, l = 1, m_l = 0, m_s = +\frac{1}{2}$

**Answer:** (a) This set is not possible because principal quantum no. (n) can not be zero

(b) This set is possible

(c) This set is not possible because for n, value of l vary from 0 to n-1 and for n=1, l=0 and 1

(d) This set is possible

(e) This set is not possible because for n, value of l vary from 0 to 3-1 i.e. 0 to 2 i.e. 0, 1, 2

(f) This set is possible

**31. How many electrons in an atom may have the following quantum numbers.**

(a)  $n = 4, m_s = -\frac{1}{2}$

(b)  $n=3, l=1$

**Answer:** (a) For value of n total no. of electrons =  $2n^2$

For  $n = 4$ , total no. of electrons =  $2(4)^2 = 32$

It is fully filled orbital as  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10}$

Thus, all electrons are paired

No. of electrons = 16

(b) Here, given values indicates that electrons are present in 3s orbital

So, no. of electrons = 2

**32. Show that the circumference of the Bohr orbit for the hydrogen atom is an integral multiple of the de Broglie wavelength associated with the electron revolving around the orbit.**

**Answer:** Here, angular momentum of electron is

$$mvr = n \frac{h}{2\pi} \quad \dots\dots(1) \quad \text{where } n = 1,2,3,\dots$$

From de Broglie's equation, we have

$$\lambda = \frac{h}{mv} \quad \text{or } mv = \frac{h}{\lambda} \quad (2)$$

Now, substitute value of  $mv$  in (1), we get

$$\frac{hr}{\lambda} = n \frac{h}{2\pi}$$

$2\pi r = n\lambda$  where  $2\pi r$  is circumference of Bohr orbit

**33. What transition in the hydrogen spectrum would have the same wavelength as the Balmer transition  $n = 4$  to  $n = 2$  of  $\text{He}^+$  spectrum.**

**Answer:** From Balmer transition  $n = 4$  to  $n = 2$  of  $\text{He}^+$  ion, wave no.  $= \bar{\nu}$  and it is given by

$$\bar{\nu} = \frac{1}{\lambda} = RZ^2 \left( \frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

Here  $n_1 = 2, n_2 = 4$

$$\text{So, } \bar{\nu} = \frac{1}{\lambda} = R(2)^2 \left( \frac{1}{4} - \frac{1}{16} \right)$$

$$= 4R \left( \frac{4-1}{16} \right)$$

$$\bar{\nu} = \frac{1}{\lambda} = \frac{3R}{4}$$

$$\lambda = \frac{4}{3R}$$

Accordingly, hydrogen have same wavelength as  $\text{He}^+$

$$R(1)^2 \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right] = \frac{3R}{4}$$

$$\left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right] = \frac{3}{4}$$

So, by hit and trail method, above equality is true only when  $n_1=1, n_2=2$

Thus, for  $n_2=2$  to  $n=1$  in hydrogen have same wavelength as Balmer transition from  $n=4$  to  $n=2$  of  $\text{He}^+$

**34. Calculate the energy required for the process**



The ionization energy for the H atom in the ground state is  $2.18 \times 10^{-18} \text{ J atom}^{-1}$ .

**Answer:** Energy is given by  $E_n = -2.18 \times 10^{-18} \left( \frac{Z^2}{n^2} \right) \text{ J}$

$$\begin{aligned} \Delta E &= E_\infty - E_1 \\ &= 0 - \left[ -2.18 \times 10^{-18} \left\{ \frac{(1)^2}{(1)^2} \right\} \right] \text{ J} \end{aligned}$$

$$\Delta E = 2.18 \times 10^{-18} \text{ J}$$

For the given condition i.e.  $\text{He}^+(s) \rightarrow \text{He}^{2+}_{(g)} + e^-$

So, electron is removed from  $n = 1$  to  $n = \infty$

$$\begin{aligned} \Delta E &= E_\infty - E_1 \\ &= 0 - \left[ -2.18 \times 10^{-18} \left\{ \frac{(2)^2}{(1)^2} \right\} \right] \end{aligned}$$

$$\Delta E = 8.72 \times 10^{-18} \text{ J}$$

**35. If the diameter of a carbon atom is 0.15 nm calculate the number of carbon atoms which can be placed side by side in a straight line across length of scale of length 20 cm long.**

**Answer:** As we know that  $1\text{m} = 100 \text{ cm}$  or  $1\text{cm} = 10^{-2}\text{m}$

$$\text{Length of scale} = 20 \text{ cm} = 20 \times 10^{-2} \text{ m}$$

$$\text{Diameter of carbon atom} = 0.15 \text{ nm} = 0.15 \times 10^{-9} \text{ m}$$

$$\text{One carbon atom contains } 0.15 \times 10^{-9} \text{ m}$$

$$\text{Now, No. of carbon atoms placed in straight line} = \frac{20 \times 10^{-2} \text{ m}}{0.15 \times 10^{-9} \text{ m}}$$

$$= 133.33 \times 10^7$$

$$= 1.33 \times 10^9$$

**36.  $2 \times 10^8$  atoms of carbon are arranged side by side. Calculate the radius of carbon atom if the length of this arrangement is 2.4 cm.**

**Answer:** Given that

$$\text{Length} = 2.4 \text{ cm}$$

$$\text{No. of carbon atoms present} = 2 \times 10^8$$

$$\text{So, diameter} = \frac{2.4 \times 10^{-2} \text{ m}}{2 \times 10^8} = 1.2 \times 10^{-10} \text{ m}$$

$$\text{This implies Radius of carbon atom} = \frac{\text{Diameter}}{2}$$

$$= \frac{1.2 \times 10^{-10} \text{ m}}{2}$$

$$= 6.0 \times 10^{-11} \text{ m}$$

**37. The diameter of zinc atom is 2.6 Å Calculate (a) radius of zinc atom in pm and (b) number of atoms present in a length of 1.6 cm if the zinc atoms are arranged side by side lengthwise.**

**Answer:** (a) Radius of zinc atom =  $\frac{\text{Diameter}}{2}$

$$= \frac{2.6 \text{ Å}}{2}$$

$$= 1.3 \times 10^{-10} \text{ m}$$

$$= 130 \times 10^{-12} \text{ m} = 130 \text{ pm}$$

(b) Length = 1.6 cm =  $1.6 \times 10^{-2} \text{ m}$

$$\text{Diameter} = 2.6 \times 10^{-10} \text{ m}$$

$$\text{No. of zinc atoms present} = \frac{1.6 \times 10^{-2} \text{ m}}{2.6 \times 10^{-10} \text{ m}}$$

$$= 0.6153 \times 10^8 \text{ m}$$

$$= 6.153 \times 10^7$$

**38. A certain particle carries  $2.5 \times 10^{-16} \text{ C}$  of static electric charge. Calculate the number of electrons present in it.**

**Answer:** As we know charge on one electron =  $1.6022 \times 10^{-19} \text{ C}$

This implies  $1.6022 \times 10^{-19} \text{ C}$  is carried by one electron

No. of electrons which carry charge of  $2.5 \times 10^{-16} \text{C}$

$$\begin{aligned}
 &= \frac{1}{1.6022 \times 10^{-19} \text{C}} (2.5 \times 10^{-16} \text{C}) \\
 &= 1.560 \times 10^3 \text{C} \\
 &= 1560 \text{C}
 \end{aligned}$$

**39. In Milikan's experiment, static electric charge on the oil drops has been obtained by shining X-rays. If the static electric charge on the oil drop is  $-1.282 \times 10^{-18} \text{C}$  calculate the number of electrons present on it.**

**Answer:** As charge on oil drop =  $1.282 \times 10^{-18} \text{C}$

Given that charge on one electron =  $1.6022 \times 10^{-19} \text{C}$

$$\begin{aligned}
 \text{No. of electrons present} &= \frac{1.282 \times 10^{-18} \text{C}}{1.6022 \times 10^{-19} \text{C}} \\
 &= 0.8001 \times 10^1 \\
 &= 8.0
 \end{aligned}$$

**40. In Rutherford's experiment, generally the thin foil of heavy atoms, like gold, platinum etc. have been used to be bombarded by the a-particles. If the thin foil of light atoms like Aluminium etc. is used, what difference would be observed from the above results?**

**Answer:** As thin foil of light atoms not give same result as foil of heavy atom

So, light atom carry positive charge

Thus, they carry deflection of a-particles which is positively charged

**41. Symbols  ${}^{79}_{35}\text{Br}$ ,  ${}^{79}\text{Br}$  can be written, whereas symbols  ${}^{35}_{79}\text{Br}$ ,  ${}^{35}\text{Br}$  are not acceptable. Answer briefly.**

**Answer:** Let us denote atomic mass = A and atomic number = Z

i.e. general convention represents as  ${}^A_Z\text{X}$

Thus,  ${}^{79}_{35}\text{Br}$  is acceptable but  ${}^{35}_{79}\text{Br}$  not acceptable

So,  ${}^{79}\text{Br}$  can be written but  ${}^{35}\text{Br}$  it can't be written because Z is constant but A depends on relative abundance of its isotopes

Thus, it is necessary to mention A

**42. An element with mass number 81 contains 31.7% more neutrons as compared to protons. Assign the atomic symbol.**

**Answer:** Let no. of protons =  $x$

So, no. of neutron =  $x + 31.7\%$  of  $x$

$$= x + 0.317x$$

$$= 1.317x$$

Now, we have given that mass no. = 81

No. of protons + no. of neutrons = 81

This implies  $x + 1.317x = 81$

$$2.317x = 81$$

$$x = \frac{81}{2.317} = 34.95$$

$$x = 35$$

As atomic no. is defined as no. of protons which is present in its nucleus

Atomic no. = 35

And atomic symbol =  ${}_{35}^{81}\text{Br}$

**43. An ion with mass number 37 possesses one unit of negative charge. If the ion contains 11.1% more neutrons than the electrons. Find the symbol of the ion.**

**Answer:** Let no. of electrons =  $x$

So, no. of neutrons =  $x + 11.1\%$  of  $x$

$$= x + 0.111x$$

$$= 1.111x$$

No. of electrons =  $(x - 1)$

So, no. of protons =  $(x - 1)$

We have given that mass no. = 37

Thus  $(x - 1) + 1.111x = 37$

$$2.111x = 38$$

$$x = 18$$

Hence symbol of the ion =  ${}_{17}^{37}\text{Cl}^-$

**44. An ion with mass number 56 possesses three unit of positive charge and 30.4% more neutrons than the electrons. Assign the symbol to this ion.**

**Answer:** Let no. of electrons in  $A^{3+}$  be  $x$

No. of neutrons =  $x + 30.4\%$  of  $x = 1.304x$

As ion is tripositive

This implies that no. of electrons in neutral atom =  $x + 3$

So, no. of protons in neutral atom =  $x + 3$

As it is given that mass no. = 56

$$(x+3) + (1.304x) = 56$$

$$2.304x = 53$$

$$x = \frac{53}{2.304}$$

$$x = 23$$

Thus, no. of protons =  $x + 3 = 23 + 3 = 26$

Hence symbol =  ${}_{26}^{56}\text{Fe}^{3+}$

**45. Arrange the following type of radiations in increasing order of frequency: (a) radiation from microwave oven (b) amber light from traffic signal (c) radiation from FM radio (d) cosmic rays from outer space and (e) X-rays.**

**Answer:** Here is the increasing order of frequency for these radiations

Radiation from FM radio < amber light < radiation from microwave oven < x-rays < cosmic rays

And here is the increasing order of wavelength for these radiations

Cosmic rays < x-rays < radiation from microwave ovens < amber light < radiation of FM radio

**46. Nitrogen laser produces a radiation at a wavelength of 337.1 nm. If the number of photons emitted is  $5.6 \times 10^{24}$  calculate the power of this laser.**

**Answer:** Here power of laser = energy which emits photons

$$\text{Power} = E = \frac{Nhc}{\lambda}$$

where  $N$  = no. of photons

$h$  = planck constant

$\lambda$  = wavelength

$c$  = velocity



Put all values to find E , we get:

$$\begin{aligned}
 E &= \frac{(5.6 \times 10^{24})(6.626 \times 10^{-34} \text{ Js})(3 \times 10^8 \text{ ms}^{-1})}{(337.1 \times 10^{-9} \text{ m})} \\
 &= 0.3302 \times 10^7 \text{ J} \\
 &= 3.33 \times 10^6 \text{ J}
 \end{aligned}$$

**47. Neon gas is generally used in the sign boards. If it emits strongly at 616 nm calculate**

- the frequency of emission
- distance travelled by this radiation in 30 s
- energy of quantum
- number of quanta present if it produces 2 J of energy.

**Answer:** We have given that wavelength = 616 nm =  $616 \times 10^{-9} \text{ m}$

(a) Let frequency of emission denotes by  $\nu$

$$\nu = \frac{c}{\lambda} \text{ where } c = \text{velocity, } \lambda = \text{wavelength}$$

$$\begin{aligned}
 \nu &= \frac{3.0 \times 10^8 \text{ m/s}}{616 \times 10^{-9} \text{ m}} \\
 &= 4.87 \times 10^8 \times 10^9 \times 10^{-3} \text{ s}^{-1} \\
 &= 4.87 \times 10^{14} \text{ s}^{-1}
 \end{aligned}$$

(b) As we know velocity (c) =  $3.0 \times 10^8 \text{ ms}^{-1}$

So, distance travelled in 30 s

$$\begin{aligned}
 &= (3.0 \times 10^8 \text{ ms}^{-1})(30 \text{ s}) \\
 &= 9.0 \times 10^9 \text{ m}
 \end{aligned}$$

(c) Energy (E) =  $h\nu$

$$\begin{aligned}
 &= (6.626 \times 10^{-34} \text{ J s})(4.87 \times 10^{14} \text{ s}^{-1}) \\
 &= 32.27 \times 10^{-20} \text{ J}
 \end{aligned}$$

(d) Energy of one photon =  $32.27 \times 10^{-20} \text{ J}$

So,  $32.27 \times 10^{-20} \text{ J}$  is present in one quantum

$$\text{No. of quanta in } 2 \text{ J} = \frac{2 \text{ J}}{32.27 \times 10^{-20} \text{ J}}$$

$$= 6.19 \times 10^{18}$$

$$= 6.2 \times 10^{18}$$

**48. In astronomical observations, signals observed from the distant stars are generally weak. If the photon detector receives a total of  $3.15 \times 10^{-18}$  J from the radiations of 600 nm calculate the number of photons received by the detector.**

**Answer:** As  $E = \frac{hc}{\lambda}$

where  $\lambda$  = wavelength

$h$  = planck constant

$c$  = velocity

Putting values we get

$$E = \frac{(6.626 \times 10^{-34} \text{ Js})(3 \times 10^8 \text{ ms}^{-1})}{(600 \times 10^{-9} \text{ m})}$$

$$= 3.313 \times 10^{-19} \text{ J}$$

$$\text{No. of photons} = \frac{3.15 \times 10^{-18} \text{ J}}{3.313 \times 10^{-19} \text{ J}} = 9.5 = 10 \text{ (approx)}$$

**49. Lifetimes of the molecules in the excited states are often measured by using pulsed radiation source of duration nearly in the nano second range. If the radiation source has the duration of 2 ns and the number of photons emitted during the pulse source is  $2.5 \times 10^{15}$  calculate the energy of the source.**

**Answer:** As frequency of radiation ( $\nu$ ) =  $\frac{1}{2.0 \times 10^{-9} \text{ s}} = 5.0 \times 10^8 \text{ s}^{-1}$

$$\text{Energy (E)} = N h \nu$$

where  $N$  = no. of photons

$h$  = planck constant

$\nu$  = frequency

Putting values we get

$$E = (2.5 \times 10^{15})(6.626 \times 10^{-34} \text{ J s})(5.0 \times 10^8 \text{ s}^{-1})$$

$$= 8.282 \times 10^{-10} \text{ J}$$

**50. The longest wavelength doublet absorption transition is observed at 589 and 589.6 nm. Calculate the frequency of each transition and energy difference between two excited states.**

**Answer:** The frequency of first transition is

$$v_1 = \frac{c}{\lambda_1} = \frac{3.0 \times 10^8}{589 \times 10^{-9}} = 5.093 \times 10^{14} \text{ s}^{-1}$$

The frequency of second transition is

$$v_2 = \frac{c}{\lambda_2} = \frac{3.0 \times 10^8}{589.6 \times 10^{-9}} = 5.088 \times 10^{14} \text{ s}^{-1}$$

The energy difference between two transitions is

$$\Delta E = h(v_2 - v_1) = 6.626 \times 10^{-34} \times (5.093 - 5.088) \times 10^{14} = 3.313 \times 10^{-22} \text{ J.}$$

**51. The work function for caesium atom is 1.9 eV Calculate**

**(a) the threshold wavelength and**

**(b) the threshold frequency of the radiation. If the caesium element is irradiated with a wavelength 500 nm**

**(c) calculate the kinetic energy and the velocity of the ejected photoelectron.**

**Answer:** Given that work  $W_0$  for caesium atom = 1.9 eV

$$(a) \text{ As } W_0 = \frac{hc}{\lambda_0} \text{ or } \lambda_0 = \frac{hc}{W_0}$$

where  $\lambda_0$  = threshold wavelength

$h$  = planck constant

$c$  = velocity

Putting values we get:

$$\lambda_0 = \frac{(6.626 \times 10^{-34} \text{ Js})(3.0 \times 10^8 \text{ ms}^{-1})}{1.9 \times 1.602 \times 10^{-19} \text{ J}}$$

$$\lambda_0 = 6.53 \times 10^{-7} \text{ m}$$

Thus, threshold wavelength  $\lambda_0 = 653 \text{ nm}$

$$(b) \text{ As } W_0 = hv_0 \text{ or } v_0 = \frac{W_0}{h}$$

where  $v_0$  = threshold frequency

$h$  = planck constant

Putting values we get:

$$v_0 = \frac{1.9 \times 1.602 \times 10^{-19} \text{ J}}{6.626 \times 10^{-34} \text{ J s}}$$

$$(\because 1 \text{ eV} = 1.602 \times 10^{-19} \text{ J})$$

$$v_0 = 4.593 \times 10^{14} \text{ s}^{-1}$$

(c) Here wavelength  $\lambda = 500 \text{ nm}$

Kinetic energy =  $h(v - v_0)$

$$= hc \left( \frac{1}{\lambda} - \frac{1}{\lambda_0} \right)$$

$$= (6.626 \times 10^{-34} \text{ Js}) (3.0 \times 10^8 \text{ ms}^{-1}) \left( \frac{\lambda_0 - \lambda}{\lambda \lambda_0} \right)$$

$$= (1.9878 \times 10^{-26} \text{ Jm}) \left[ \frac{(653 - 500) 10^{-9} \text{ m}}{(653)(500) 10^{-18} \text{ m}^2} \right]$$

$$= \frac{(1.9878 \times 10^{-26}) (153 \times 10^9)}{(653)(500)} \text{ J}$$

$$= 9.3149 \times 10^{-20} \text{ J}$$

So, kinetic energy of ejected photoelectron =  $9.3149 \times 10^{-20} \text{ J}$

$$\text{As K.E.} = \frac{1}{2} mv^2 = 9.3149 \times 10^{-20} \text{ J}$$

$$v = \sqrt{\frac{2(9.3149 \times 10^{-20} \text{ J})}{9.10939 \times 10^{-31} \text{ kg}}}$$

$$= \sqrt{2.0451 \times 10^{11} \text{ m}^2 \text{ s}^{-2}}$$

$$v = 4.52 \times 10^5 \text{ ms}^{-1}$$

**52. Following results are observed when sodium metal is irradiated with different wavelengths. Calculate (a) threshold wavelength and, (b) Planck's constant.**

$\lambda$ (nm)	500	450	400
$v \times 10^{-5}$ ( $\text{cm s}^{-1}$ )	2.55	4.35	5.35

**Answer:** Let threshold wavelength  $\lambda_0$  nm ( $= \lambda_0 \times 10^{-9}$  m)

Kinetic energy is

$$h(v - v_0) = \frac{1}{2}mv^2$$

From this three different equalities it formed

$$hc \left( \frac{1}{\lambda} - \frac{1}{\lambda_0} \right) = \frac{1}{2}mv^2$$

$$hc \left( \frac{1}{500 \times 10^9} - \frac{1}{\lambda_0 \times 10^9 \text{ m}} \right) = \frac{1}{2}m(2.55 \times 10^5 \times 10^{-2} \text{ ms}^{-1})$$

$$\frac{hc}{10^9 \text{ m}} \left[ \frac{1}{500} - \frac{1}{\lambda_0} \right] = \frac{1}{2}m(2.55 \times 10^3 \text{ ms}^{-1})^2 \quad \text{(i)}$$

Similarly,

$$\frac{hc}{10^9 \text{ m}} \left[ \frac{1}{450} - \frac{1}{\lambda_0} \right] = \frac{1}{2}m(3.45 \times 10^3 \text{ ms}^{-1})^2 \quad \text{(ii)}$$

$$\frac{hc}{10^9 \text{ m}} \left[ \frac{1}{400} - \frac{1}{\lambda_0} \right] = \frac{1}{2}m(5.35 \times 10^3 \text{ ms}^{-1})^2 \quad \text{(iii)}$$

Divide (iii) by (i) we get:

$$\frac{\left[ \frac{\lambda_0 - 400}{400\lambda_0} \right]}{\left[ \frac{\lambda_0 - 500}{500\lambda_0} \right]} = \frac{(5.35 \times 10^3 \text{ ms}^{-1})^2}{(2.55 \times 10^3 \text{ ms}^{-1})^2}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = \left( \frac{5.35}{2.55} \right)^2 = \frac{28.6225}{6.5025}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = 4.40177$$

$$17.6070\lambda_0 - 5\lambda_0 = 8803.537 - 2000$$

$$\lambda_0 = \frac{6805.537}{12.607}$$

$$\lambda_0 = 539.8 \text{ nm}$$

$$\lambda_0 = 540 \text{ nm}$$

**53. The ejection of the photoelectron from the silver metal in the photoelectric effect experiment can be stopped by applying the voltage of 0.35 V when the radiation 256.7 nm is used. Calculate the work function for silver metal.**

**Answer:** Let  $E$  = energy,  $W_0$  = work function

So, by principle of conservation:

$$E = W_0 + \text{K.E.}$$

$$\text{or } W_0 = E - \text{K.E.}$$

$$\therefore E = \frac{hc}{\lambda}$$

Putting all values we get:

$$E = \frac{(6.626 \times 10^{-34} \text{ Js})(3.0 \times 10^8 \text{ ms}^{-1})}{256.7 \times 10^{-9} \text{ m}}$$

$$= 7.744 \times 10^{-19} \text{ J} = \frac{7.744 \times 10^{-19}}{1.602 \times 10^{-19}} \text{ eV}$$

$$E = 4.83 \text{ eV}$$

Potential applied to silver metal change into kinetic energy

$$\text{K.E.} = 0.35 \text{ V} = 0.35 \text{ eV}$$

$$W_0 = E - \text{K.E.}$$

$$= 4.83 \text{ eV} - 0.35 \text{ eV}$$

$$= 4.48 \text{ eV}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = \left(\frac{5.35}{2.55}\right)^2 = \frac{28.6225}{6.5025}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = 4.40177$$

$$17.6070\lambda_0 - 5\lambda_0 = 8803.537 - 2000$$

$$\lambda_0 = \frac{6805.537}{12.607} = 539.8 \text{ nm} = 540 \text{ nm}$$

**54. If the photon of the wavelength 150 pm strikes an atom and one of its inner bound electrons is ejected out with a velocity of  $0.5 \times 10^7 \text{ ms}^{-1}$  calculate the energy with which it is bound to the nucleus.**

**Answer:** Energy ( $E$ ) =  $\frac{hc}{\lambda}$

$$= \frac{(6.626 \times 10^{-34} \text{ Js})(3.0 \times 10^8 \text{ ms}^{-1})}{(150 \times 10^{-12} \text{ m})}$$

$$= 1.3252 \times 10^{-15} \text{ J}$$

$$= 13.252 \times 10^{-16} \text{ J}$$

$$\begin{aligned}
 \text{K.E.} &= \frac{1}{2} m_e v^2 \\
 &= \frac{1}{2} (9.10939 \times 10^{-31} \text{ kg}) (1.5 \times 10^7 \text{ ms}^{-1})^2 \\
 &= 10.2480 \times 10^{-17} \text{ J} \\
 &= 1.025 \times 10^{-16} \text{ J}
 \end{aligned}$$

So, energy with which electron is bound = E - K.E.

$$\begin{aligned}
 &= 13.252 \times 10^{-16} \text{ J} - 1.025 \times 10^{-16} \text{ J} \\
 &= 12.227 \times 10^{-16} \text{ J} \\
 &= \frac{12.227 \times 10^{-16}}{1.602 \times 10^{-19}} \text{ eV} \\
 &= 7.6 \times 10^3 \text{ eV}
 \end{aligned}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = \left( \frac{5.35}{2.55} \right)^2 = \frac{28.6225}{6.5025}$$

$$\frac{5\lambda_0 - 2000}{4\lambda_0 - 2000} = 4.40177$$

$$17.6070 \lambda_0 - 5 \lambda_0 = 8803.537 - 2000$$

$$\lambda_0 = \frac{6805.537}{12.607}$$

$$\lambda_0 = 539.8 \text{ nm}$$

$$\lambda_0 = 540 \text{ nm}$$

**55. Emission transitions in the Paschen series end at orbit  $n=3$  and start from orbit  $n$  and can be represented as  $\nu = 3.29 \times 10^{15} \text{ (Hz)} \left[ \frac{1}{3^2} - \frac{1}{n^2} \right]$ . Calculate the value of  $n$  if the transition is observed at 1285 nm. Find the region of the spectrum.**

**Answer:** It is given that wavelength = 1285 nm =  $1285 \times 10^{-9} \text{ m}$

$$\nu = 3.29 \times 10^{15} \left( \frac{1}{3^2} - \frac{1}{n^2} \right)$$

$$\begin{aligned}
 \therefore \nu &= \frac{c}{\lambda} = \frac{3.0 \times 10^8 \text{ ms}^{-1}}{1285 \times 10^{-9} \text{ m}} \\
 &= 2.33 \times 10^{14} \text{ s}^{-1}
 \end{aligned}$$

Substitute value of  $\nu$  in given equation

$$3.29 \times 10^{15} \left( \frac{1}{9} - \frac{1}{n^2} \right) = 2.33 \times 10^{14}$$

$$\frac{1}{9} - \frac{1}{n^2} = \frac{2.33 \times 10^{14}}{3.29 \times 10^{15}}$$

$$\frac{1}{9} - 0.7082 \times 10^{-1} = \frac{1}{n^2}$$

$$\frac{1}{n^2} = 1.1 \times 10^{-1} - 0.7082 \times 10^{-1}$$

$$\frac{1}{n^2} = 4.029 \times 10^{-2}$$

$$n = \sqrt{\frac{1}{4.029 \times 10^{-2}}}$$

$$n = 4.98 = 5$$

So, spectrum lie in infra-red region

**56. Calculate the wavelength for the emission transition if it starts from the orbit having radius 1.3225 nm and ends at 211.6 pm Name the series to which this transition belongs and the region of the spectrum.**

**Answer:** We have given that

$$\begin{aligned}
 r &= \frac{0.529n^2}{Z} \text{ \AA} \\
 &= \frac{52.9n^2}{Z} \text{ pm}
 \end{aligned}$$

Now, for radius ( $r_1$ ) = 1.3225 nm =  $1.32225 \times 10^{-9}$  m

$$= 1322.25 \times 10^{-12} \text{ m} = 1322.25 \text{ pm}$$

$$n_1^2 = \frac{r_1 Z}{52.9} = \frac{1322.25 Z}{52.9}$$

Similarly

$$n_2^2 = \frac{211.6 Z}{52.9}$$

$$\frac{n_1^2}{n_2^2} = \frac{1322.5}{211.6}$$

$$\frac{n_1^2}{n_2^2} = 6.25$$

$$\frac{n_1}{n_2} = 2.5 = \frac{25}{10} = \frac{5}{2}$$



So, we get  $n_1 = 5, n_2 = 2$

Hence, transition vary from fifth orbit to second orbit

$$\text{So, wave number } (\bar{\nu}) = 1.097 \times 10^7 \left( \frac{1}{2^2} - \frac{1}{5^2} \right) \text{m}^{-1}$$

$$= 1.097 \times 10^7 \text{ m}^{-1} \left( \frac{21}{100} \right)$$

$$= 2.303 \times 10^6 \text{ m}^{-1}$$

$$\text{Hence wavelength } \lambda = \frac{1}{\bar{\nu}}$$

$$= \frac{1}{2.303 \times 10^6 \text{ m}^{-1}}$$

$$= 0.434 \times 10^{-6} \text{ m}$$

$$= 434 \text{ nm}$$

**57. Dual behaviour of matter proposed by de Broglie led to the discovery of electron microscope often used for the highly magnified images of biological molecules and other type of material. If the velocity of the electron in this microscope is  $1.6 \times 10^6 \text{ ms}^{-1}$  calculate de Broglie wavelength associated with this electron.**

**Answer:** According to question by de Broglie's equation, we get

$$\lambda = \frac{h}{mv}$$

$$\lambda = \frac{6.626 \times 10^{-34} \text{ Js}}{(9.10939 \times 10^{-31} \text{ kg})(1.6 \times 10^6 \text{ ms}^{-1})}$$

$$= 4.55 \times 10^{-10} \text{ m}$$

$$= 455 \text{ pm}$$

**58. Similar to electron diffraction, neutron diffraction microscope is also used for the determination of the structure of molecules. If the wavelength used here is 800 pm calculate the characteristic velocity associated with the neutron.**

**Answer:** By using de Broglie's equation, we get

$$\lambda = \frac{h}{mv} \text{ or } v = \frac{h}{m\lambda}$$

where  $v$  = velocity

$h$  = planck constant

$m$  = mass

$\lambda$  = wavelength

Putting all values we get:

$$\begin{aligned}
 v &= \frac{6.626 \times 10^{-34} \text{ Js}}{(1.67493 \times 10^{-27} \text{ kg})(800 \times 10^{-12} \text{ m})} \\
 &= 4.94 \times 10^2 \text{ ms}^{-1} \\
 &= 494 \text{ ms}^{-1}
 \end{aligned}$$

**59. If the velocity of the electron in Bohr's first orbit is  $2.19 \times 10^6 \text{ ms}^{-1}$  calculate the de Broglie wavelength associated with it.**

**Answer:** By using de Broglie's equation, we get

$$\lambda = \frac{h}{mv}$$

where  $v$  = velocity

$h$  = planck constant

$m$  = mass

$\lambda$  = wavelength

Putting all values we get:

$$\begin{aligned}
 \lambda &= \frac{6.626 \times 10^{-34} \text{ Js}}{(9.10939 \times 10^{-31} \text{ kg})(2.19 \times 10^6 \text{ ms}^{-1})} \\
 &= 3.32 \times 10^{-10} \text{ m} \\
 &= 3.32 \times 10^{-10} \text{ m} \times \frac{100}{100} \\
 &= 332 \times 10^{-12} \text{ m} \\
 &= 332 \text{ pm}
 \end{aligned}$$

**60. The velocity associated with a proton moving in a potential difference of 1000 V is  $4.37 \times 10^5 \text{ ms}^{-1}$ . If the hockey ball of mass 0.1 kg is moving with this velocity, calculate the wavelength associated with this velocity.**

**Answer:** From de Broglie expression we get

$$\begin{aligned}
 \lambda &= \frac{h}{mv} \\
 &= \frac{6.626 \times 10^{-34} \text{ Js}}{(0.1 \text{ kg})(4.37 \times 10^5 \text{ ms}^{-1})} \\
 &= 1.516 \times 10^{-38} \text{ m}
 \end{aligned}$$

**61. If the position of the electron is measured within an accuracy of +0.002 nm calculate the uncertainty in the momentum of the electron. Suppose the momentum of the electron is**

**$\frac{h}{4} \text{ nm} \times 0.05 \text{ nm}$  is there any problem in defining this value.**

**Answer:** According to Heisenberg's uncertainty principle

$$\begin{aligned}
 \Delta x \times \Delta p &= \frac{h}{4\pi} \\
 \Delta p &= \frac{1}{\Delta x} \times \frac{h}{4\pi}
 \end{aligned}$$

where  $\Delta x$  = uncertainty in position of electron

$\Delta p$  = uncertainty in momentum of electron

Put values we get:

$$\begin{aligned}
 \Delta p &= \frac{1}{0.002 \text{ nm}} \times \frac{6.626 \times 10^{-34} \text{ Js}}{4 \times (3.14)} \\
 &= \frac{1}{2 \times 10^{-12} \text{ m}} \times \frac{6.626 \times 10^{-34} \text{ Js}}{4 \times 3.14} \\
 &= 2.637 \times 10^{-23} \text{ Jsm}^{-1} \\
 \Delta p &= 2.637 \times 10^{-23} \text{ kgms}^{-1} \quad (1 \text{ J} = 1 \text{ kgms}^2 \text{ s}^{-1})
 \end{aligned}$$

$$\text{Now, actual momentum} = \frac{h}{4\pi_m \times 0.05 \text{ nm}}$$

$$\begin{aligned}
 &= \frac{6.626 \times 10^{-34} \text{ Js}}{4 \times 3.14 \times 5.0 \times 10^{-11} \text{ m}} \\
 &= 1.055 \times 10^{-24} \text{ kgms}^{-1}
 \end{aligned}$$

As magnitude of actual momentum is smaller than uncertainty

Thus, value can't be defined.

**62. The quantum numbers of six electrons are given below. Arrange them in order of increasing energies. If any of these combination(s) has/have the same energy lists:**

1.  $n = 4, l = 2, m_l = -2, m_s = \frac{-1}{2}$

2.  $n = 3, l = 2, m_l = 1, m_s = \frac{1}{2}$

3.  $n = 4, l = 1, m_l = 0, m_s = \frac{1}{2}$

4.  $n = 3, l = 2, m_l = -2, m_s = \frac{-1}{2}$

5.  $n = 3, l = 1, m_l = -1, m_s = \frac{1}{2}$

6.  $n = 4, l = 1, m_l = 0, m_s = \frac{1}{2}$

**Answer:** Here,

For  $n = 4, l = 2$ , orbital occupied = 4d

For  $n = 3, l = 2$ , orbital occupied = 3d

For  $n = 4, l = 1$ , orbital occupied = 4p

Thus, six electrons i.e. 1,2,3,4,5,6 are present in 4d, 3d, 4p, 3d, 3p, 4p orbitals respectively

So, increasing order is  $5(3p) < 2(3d) = 4(3d) < 3(4p) = 6(4p) < 1(4d)$

**63. The bromine atom possesses 35 electrons. It contains 6 electrons in 2p orbital, 6 electrons in 3p orbital and 5 electrons in 4p orbital. Which of these electron experiences the lowest effective nuclear charge?**

**Answer:** Nuclear charge experienced by electron is dependent on the distance between nucleus and orbital where electron is present. Since distance increases, so effective nuclear charge also decreases. Further p-orbitals, 4p orbitals are farthest from nucleus of bromine atom with +35 charge. Thus, electrons in 4p orbital experience lowest effective nuclear charge and these electrons are shielded by electrons which are present in 2p, 3p orbitals with s-orbitals. So, they will experience lowest nuclear charge.

**64. Among the following pairs of orbitals which orbital will experience the larger effective nuclear charge?**

(i) 2s and 3s

(ii) 4d and 4f

(iii) 3d and 3p

**Answer:** (i) Electrons present in  $2s$  orbital will experience larger effective nuclear charge as compared to the electrons in  $3s$  orbital because it is closer to the nucleus

(ii) Electrons present in  $4d$  orbital will experience larger effective nuclear charge as compared to the electrons in  $4f$  orbital because it is closer to the nucleus

(iii) Electrons present in  $3p$  orbital will experience larger effective nuclear charge as compared to the electrons in  $3f$  orbital because it is closer to the nucleus

**65. The unpaired electrons in Al, Si are present in  $3p$  orbital. Which electrons will experience more effective nuclear charge from the nucleus?**

**Answer:** Higher atomic number will get higher nuclear charge. As we know Silicon has 14 protons while aluminium has 13 protons. Thus, from this we get that silicon has larger nuclear charge i.e. +14 than aluminium which has nuclear charge +13. Hence, electrons in  $3p$  orbital of silicon will experience more effective nuclear charge than aluminium.

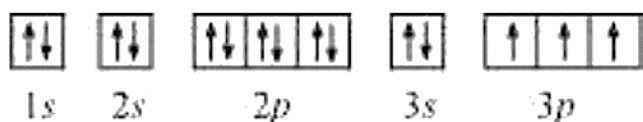
**66. Indicate the number of unpaired electrons in:**

- (a) P
- (b) Si
- (c) Cr
- (d) Fe
- (e) Kr

**Answer:** (a) Atomic no. = 15

Electronic configuration of P =  $1s^2 2s^2 2p^6 3s^2 3p^3$

Orbital picture of P

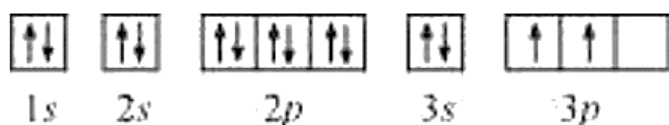


Thus, phosphorus has 3 unpaired electrons

(b) Atomic no. = 14

Electronic configuration of Si =  $1s^2 2s^2 2p^6 3s^2 3p^2$

Orbital picture of Si

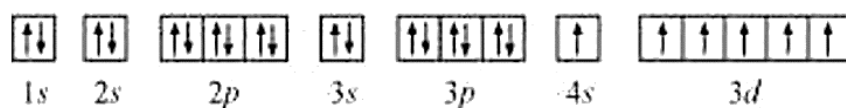


Thus, silicon has 2 unpaired electrons

(c) Atomic no. = 24

Electronic configuration of Cr =  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^1 3d^5$

Orbital picture of Cr

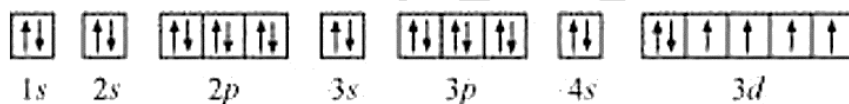


Thus, chromium has 6 unpaired electrons

(d) Atomic no. = 26

Electronic configuration of Fe =  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^6$

Orbital picture of Fe

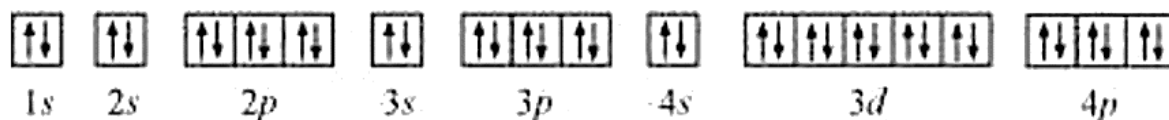


Thus, Iron has 4 unpaired electrons

(e) Atomic no. = 36

Electronic configuration of Kr =  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6$

Orbital picture of Kr



Thus, krypton are fully occupied, so no unpaired electrons.

**67. (a) How many sub-shells are associated with n=4**

(b) How many electrons will be present in the sub-shells having  $m_s$  value of  $-\frac{1}{2}$  for  $n=4$ .

**Answer:** (a) Given that  $n = 4$

For given values of  $n$ ,  $l$  have values from 0 to  $(n-1)$

So,  $l = 0, 1, 2, 3$

Hence, 4 sub shells associated with  $n = 4$  i.e. s, p, d, f

(b) No. of orbital in  $n^{\text{th}}$  shell =  $n^2$

For  $n = 4$

No. of orbitals = 16

If orbital is fully taken, then it have one electron with  $m_s$  value of  $-\frac{1}{2}$

So, no. of electrons = 16