VITEEE 2022 Question Paper

Time Allowed :2 hours 30 minutesMaximum Marks :125Total questions :125

General Instructions

Read the following instructions very carefully and strictly follow them :

- 1. This question paper contains 125 questions. All questions are compulsory.
- 2. There are 5 sections in the question paper- Mathematics, Physics, Chemistry, Aptitude, English.
- 3. There are 35 questions each in Chemistry and Physics, 40 questions in Mathematics, 10 question of Aptitude, and 5 questions of English.
- 4. 1 mark will be given for each correct answer. There is no negative marking. No marks will be deducted for any wrong response selected by candidates.

Physics

1. The root mean square speed of smoke particles of mass 5×10^{-17} kg in their Brownian motion in air at NTP is approximately. (Given $k = 1.38 \times 10^{-23}$ JK⁻¹)

(A) 60 mm/s

(B) 12 mm/s

(C) 15 mm/s

(D) 36 mm/s

2. The equation of a particle executing simple harmonic motion is given by

$$x = \sin \pi \left(t + \frac{1}{3} \right) \,\mathbf{m}.$$

At t = 1 s, the speed of particle will be (Given $\pi = 3.14$):

- (A) $0 \,\mathrm{cm} \,\mathrm{s}^{-1}$
- (B) $157 \,\mathrm{cm} \,\mathrm{s}^{-1}$
- (C) 272 cm s^{-1}
- (D) 314 cm s^{-1}

3. Following are expressions for four plane simple harmonic waves

$$y_1 = A \cos 2\pi \left(n_1 t + \frac{x}{\lambda_1} \right),$$

$$y_2 = A \cos 2\pi \left(n_1 t + \frac{x}{\lambda_1} + \pi \right),$$

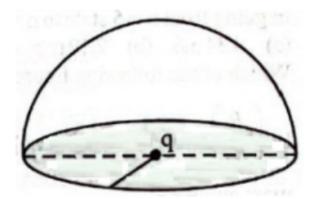
$$y_3 = A \cos 2\pi \left(n_2 t + \frac{x}{\lambda_2} \right),$$

$$y_4 = A \cos 2\pi \left(n_2 t - \frac{x}{\lambda_2} \right)$$

The pairs of waves which will produce destructive interference and stationary waves respectively in a medium, are

- (A) (iii), (iv), (i), (ii)(B) (i), (iii), (ii), (iv)
- $(C)\,(i),\,(iv),\,(ii),\,(iii)$
- (D) (i), (ii), (iii), (iv)

4. If a charge *q* is placed at the centre of a closed hemispherical non-conducting surface, the total flux passing through the flat surface would



- (A) zero
- (B) $\frac{q}{2\epsilon_0}$

(C) $\frac{q}{4\epsilon_0}$

(D) $\frac{q}{2\pi\epsilon_0}$

5. The electric potential V(x) in a region around the origin is given by $V(x) = 4x^2$ volts.

The electric charge enclosed in a cube of 1m side with its center at the origin is (in coulomb)

- (A) $8\epsilon_0$
- (B) $-4\epsilon_0$
- (C) 0
- (D) $-8\epsilon_0$

6. A heater coil is cut into two equal parts and only one part is now used in the heater. The heat generated will now be

- (A) four times
- (B) doubled
- (C) halved
- (D) one fourth

7. In a region, steady and uniform electric and magnetic fields are present. These two fields are parallel to each other. A charged particle is released from rest in this region. The path of the particle will be a

(A) helix

(B) straight line

(C) ellipse

(D) circle

8. An object is thrown vertically upwards. At its maximum height, which of the following quantity becomes zero?

- (A) Momentum
- (B) Potential energy
- (C) Acceleration
- (D) Force

9. The self-induced emf of a coil is 25 volts. When the current in it is changed at uniform rate from 10A to 25 A in 1s, the change in the energy of the inductance is:

(A) 740J

(B) 437.5J

- (C) 540J
- (D) 637.5J

10. Alternating current cannot be measured by a D.C. ammeter because

- (A) Average value of current for complete cycle is zero
- (B) A.C. Changes direction
- (C) A.C. cannot pass through D.C. Ammeter
- (D) D.C. Ammeter will get damaged.

11. The magnetic field of a plane electromagnetic wave is given by:

$$\vec{B} = 2 \times 10^{-8} \sin \left(0.5 \times 10^3 x + 1.5 \times 10^{11} t \right) \hat{j} \,\mathrm{T}.$$

The amplitude of the electric field would be:

- (A) 6 V/m along x-axis
- (B) 3 V/m along z-axis
- (C) 6 V/m along z-axis
- (D) 2×10^{-8} V/m along z-axis

12. An ideal gas is expanding such that $PT^3 = \text{constant}$. The coefficient of volume expansion of the gas is:

- (A) $\frac{1}{T}$
- (B) $\frac{2}{T}$
- (C) $\frac{4}{T}$
- (D) $\frac{3}{T}$

13. Two light beams of intensities in the ratio of 9 : 4 are allowed to interfere. The ratio of the intensity of maxima and minima will be:

- (A) 2 : 3
- (B) 16:81
- (C) 25 : 169
- (D) 25 : 1

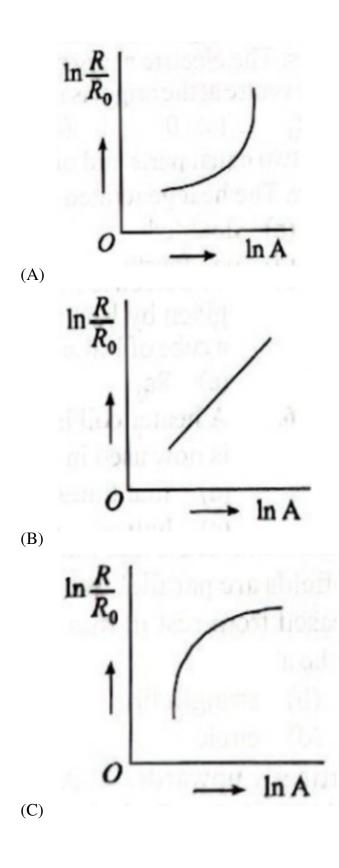
14. The de Broglie wavelength of a proton and α -particle are equal. The ratio of their velocities is:

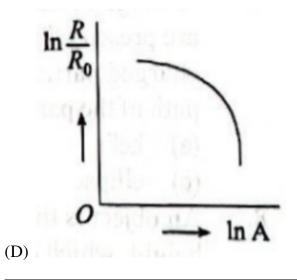
- (A) 4 : 3
- **(B)** 4 : 1
- (C) 4 : 2
- (D) 1 : 4

15. The recoil speed of a hydrogen atom after it goes from n = 5 state to n = 1 state will be:

- (A) 4.34 m/s
- (B) 2.19 m/s
- (C) 4.17 m/s
- (D) 3.25 m/s

16. Which of the following figure represents the variation of $\ln \left(\frac{R}{R_0}\right)$ with $\ln A$ (If R is the radius of a nucleus and A is its mass number)?





17. Zener breakdown occurs in a p n junction having p and n both:

- (A) lightly doped and have wide depletion layer
- (B) heavily doped and have narrow depletion layer
- (C) lightly doped and have narrow depletion layer
- (D) heavily doped and have wide depletion layer

18. If *E* and *H* represent the intensity of electric field and magnetizing field respectively, then the unit of $\frac{E}{H}$ will be:

- (A) ohm
- (B) mho
- (C) joule
- (D) newton

19. A stone of mass *m*, tied to a string is being whirled in a vertical circle with a uniform speed. The tension in the string is:

- (A) the same throughout the motion
- (B) minimum at the highest position of the circular path
- (C) minimum at the lowest position of the circular path
- (D) minimum when the rope is in the horizontal position

20. A particle is moving with a velocity $\vec{v} = K(y\hat{i} + x\hat{j})$, where K is a constant. The

general equation for its path is:

(A) $y = x^2 + \text{constant}$ (B) $y^2 = x + \text{constant}$ (C) $y^2 = x^2 + \text{constant}$ (D) xy = constant

21. A particle of mass M originally at rest is subjected to a force whose direction is constant but magnitude varies with time according to the relation

$$F = F_0 \left[1 - \left(\frac{t-T}{T}\right)^2 \right]$$

Where F_0 and T are constants. The force acts only for the time interval 2T. The velocity v of the particle after time 2T is:

(A) $\frac{2F_0T}{M}$

(B) $\frac{F_0T}{2M}$

- (C) $\frac{4F_0T}{3M}$
- (D) $\frac{F_0 T}{3M}$

22. The magnetic moment of an electron (e) revolving in an orbit around nucleus with an orbital angular momentum is given by:

(A) $\vec{\mu}_L = \frac{e\vec{L}}{2m}$ (B) $\vec{\mu}_L = -\frac{e\vec{L}}{2m}$ (C) $\vec{\mu}_l = -\frac{e\vec{L}}{m}$ (D) $\vec{\mu}_l = \frac{2e\vec{L}}{m}$

23. Angular momentum of the particle rotating with a central force is constant due to

- (A) constant torque
- (B) constant force
- (C) constant linear momentum
- (D) zero torque

24. The escape velocity of a body depends upon mass as:

(A) m⁰
(B) m¹
(C) m²
(D) m³

25. Potential energy as a function of r is given by $U = \frac{A}{r^{10}} - \frac{B}{r^5}$, where r is the interatomic distance, A and B are positive constants. The equilibrium distance between the two atoms will be:

(A) $\left(\frac{A}{B}\right)^{\frac{1}{5}}$

- (B) $\left(\frac{B}{A}\right)^{\frac{1}{5}}$ (C) $\left(\frac{2A}{B}\right)^{\frac{1}{5}}$
- (D) $\left(\frac{B}{2A}\right)^{\frac{1}{5}}$

26. If two soap bubbles of different radii are connected by a tube:

(A) air flows from the smaller bubble to the bigger bubble

(B) air flows from the bigger bubble to the smaller bubble till the sizes are interchanged

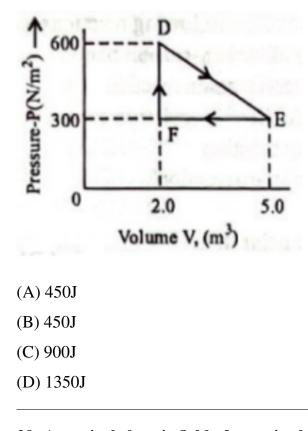
(C) air flows from the bigger bubble to the smaller bubble till the sizes become equal

(D) there is no flow of air.

27. The focal length *f* is related to the radius of curvature *r* of the spherical convex mirror by:

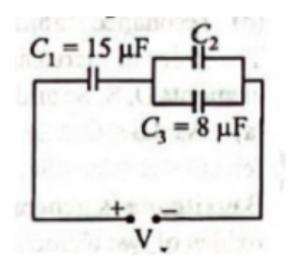
(A) $f = +\frac{r}{2}$ (B) f = -r(C) $f = -\frac{r}{2}$ (D) f = r

28. A thermodynamic system is taken from an original state D to an intermediate state E by the linear process shown in the figure. Its volume is then reduced to the original volume from E to F by an isobaric process. The total work done by the gas from D to E to F will be:



29. A vertical electric field of magnitude 4.9×10^5 N/C just prevents a water droplet of a mass 0.1 g from falling. The value of charge on the droplet will be: (Given g = 9.8 m/s²) (A) 1.6×10^{-9} C (B) 2.0×10^{-9} C (C) 3.2×10^{-9} C (D) 0.5×10^{-9} C

30. In the circuit shown in the figure, the total charge is $750 \mu C$ and the voltage across capacitor C_2 is 20 V. Then the charge on capacitor C_2 is:



- (A) 450 μC
- **(B)** 590 μC
- (**C**) 160 µC
- **(D)** 650 μC

31. For a transistor, α and β are given as $\alpha = \frac{I_C}{I_E}$ and $\beta = \frac{I_C}{I_B}$. Then the correct relation between α and β will be:

- (A) $\alpha = \frac{1-\beta}{\beta}$ (B) $\beta = \frac{\alpha}{1-\alpha}$
- (C) $\alpha\beta = 1$
- (D) $\alpha = \frac{\beta}{1-\beta}$

32. A current *I* flows along the length of an infinitely long, straight, thin-walled pipe.

Then:

- (A) the magnetic field at all points inside the pipe is the same, but not zero
- (B) the magnetic field is zero only on the axis of the pipe
- (C) the magnetic field is different at different points inside the pipe
- (D) the magnetic field at any point inside the pipe is zero

33. A Carnot engine has an efficiency of 50%. If the temperature of the sink is reduced by 40°C, its efficiency increases by 30%. The temperature of the source will be:
(A) 166.7K

(B) 255.1K

(C) 266.7K

(D) 367.7K

34. When you walk through a metal detector carrying a metal object in your pocket, it raises an alarm. This phenomenon works on:

(A) Electromagnetic induction

- (B) Resonance in ac circuits
- (C) Mutual induction in ac circuits
- (D) Interference of electromagnetic waves

35. An electron moving with speed v and a photon with speed c, have the same

de-Broglie wavelength. The ratio of kinetic energy of the electron to that of the photon

is:

(A) $\frac{3c}{v}$

(B) $\frac{v}{3c}$

(C) $\frac{v}{2c}$

(D) $\frac{2c}{v}$

Chemistry

36. Assuming fully decomposed, the volume of CO₂ released will be:

- (A) 1.12L
- (B) 2.24L
- (C) 4.06L
- (D) 0.84L

37. Among the following, the species having the smallest bond order is:

 $(A) NO^{-}$

 $(B) NO^+$

 $(\mathbf{C})\,\mathbf{O}_2$

38. The oxidation number of phosphorus in $Ba(H_2PO_2)_2$ is:

(A) + 3

(B) + 2

(C) +1

(D) -1

39. The correct order of thermal stability of hydroxides is:

 $\begin{array}{l} (A) \ Ba(OH)_2 < Ca(OH)_2 < Sr(OH)_2 < Mg(OH)_2 \\ (B) \ Mg(OH)_2 < Sr(OH)_2 < Ca(OH)_2 < Ba(OH)_2 \\ (C) \ Mg(OH)_2 < Ca(OH)_2 < Sr(OH)_2 < Ba(OH)_2 \\ (D) \ Ba(OH)_2 < Sr(OH)_2 < Ca(OH)_2 < Mg(OH)_2 \end{array}$

40. Which of the following has correct increasing basic strength?

 $(A) MgO < BeO < CaO < BaO \\ (B) BeO < MgO < CaO < BaO \\ (C) BaO < CaO < MgO < BeO \\ (D) CaO < BaO < BeO < MgO \\$

41. Water sample is reported to be highly polluted if BOD (Biological Oxygen Demand) value of sample becomes:

- (A) more than 17 ppm.
- (B) equal to 10 ppm.
- (C) equal to 5 ppm.
- (D) less than 5 ppm.

42. 200 mL of an aqueous solution of a protein contains 1.26 g. The osmotic pressure of this solution at 300 K is found to be 2.57×10^{-3} bar. The molar mass of the protein will be: (R = 0.083 L bar mol⁻¹ K⁻¹)

(A) 51022 g/mol

(B) 122044 g/mol

(C) 31011 g/mol

(D) 61038 g/mol

43. Lyophilic sols are more stable than lyophobic sols because:

(A) the colloidal particles have positive charge

- (B) the colloidal particles have negative charge
- (C) the colloidal particles are solvated
- (D) there is strong electrostatic repulsion between the colloidal particles

44. Which of the following is not a permissible arrangement of electrons in an atom?

(A) $n = 5, l = 3, m = 0, s = +\frac{1}{2}$ (B) $n = 3, l = 2, m = -3, s = -\frac{1}{2}$ (C) $n = 3, l = 2, m = -2, s = -\frac{1}{2}$ (D) $n = 4, l = 0, m = 0, s = -\frac{1}{2}$

45. The value of van der Waals constant ' a ' for gases $\mathbf{O}_2, \mathbf{N}_2, \mathbf{NH}_3,$ and \mathbf{CH}_4 are 1.360,

1.390, 4.170, and 2.253 L²atm/mol² respectively. The gas which can most easily be liquefied is:

 $(A) O_2$

 $(B) N_2$

- $(C) NH_3$
- (D) CH₄

46. Which one of the following does not have a pyramidal shape?

- $(A) (CH_3)_3 N$
- (B) $(SiH_3)_3N$
- (C) $P(CH_3)_3$
- (D) $P(SiH_3)_3$

47. Boric acid is polymeric due to:

(A) its acidic nature

(B) the presence of hydrogen bonds

- (C) its monobasic nature
- (D) its geometry

48. Which of the following order is not correct?

- (A) $MeBr > Me_2CHBr > Me_3CBr > Et_3CBr$ (SN2)
- (B) $PhCH_2Br > PhCHBrMe > PhCBrMe_2 > PhCBrMePh$ (SN1)
- (C) MeI > MeBr > MeCl > MeF (SN2)
- (D) All are correct

49. A catalyst is a substance which:

- (A) is always in the same phase as in the reaction
- (B) alters the equilibrium in a reaction
- (C) does not participate in the reaction but alters the rate of reaction
- (D) participates in the reaction and provides an easier pathway for the same

50. Which of the following is a non-reducing sugar?

- (A) Lactose
- (B) Fructose
- (C) Sucrose
- (D) Maltose

51. An ideal gas expands against a constant external pressure of 2.0 atmosphere from 20 litre to 40 litre and absorbs 10 kJ of heat from the surrounding. What is the change

in internal energy of the system? (given: 1 atm-litre = 101.3 J)

- (A) 4052 J
- (B) 5948 J
- (C) 14052 J
- (D) 9940 J

52. The polymer used for optical lenses is:

- (A) polypropylene
- (B) polyvinyl chloride

(C) polythene

(D) polymethyl methacrylate

53. Which of the following order is not correct for the ionic radii of the given species:

 $\begin{array}{l} \mathbf{O}^{2-}, \mathbf{S}^{2-}, \mathbf{N}^{3-}, \mathbf{P}^{3-} \mathbf{?} \\ (A) \ \mathbf{O}^{2-} < \mathbf{N}^{3-} < \mathbf{S}^{2-} < \mathbf{P}^{3-} \\ (B) \ \mathbf{O}^{2-} < \mathbf{P}^{3-} < \mathbf{N}^{3-} < \mathbf{S}^{2-} \\ (C) \ \mathbf{N}^{3-} < \mathbf{O}^{2-} < \mathbf{P}^{3-} < \mathbf{S}^{2-} \\ (D) \ \mathbf{N}^{3-} < \mathbf{S}^{2-} < \mathbf{O}^{2-} < \mathbf{P}^{3-} \end{array}$

54. The IUPAC name of the following compound is:

$$CH_3 = C = C + CH_2CH_3$$

- (A) (E)-2-hepten-4-yne
- (B) (Z)-5-hepten-3-yne
- (C) (E)-5-hepten-3-yne
- (D) (Z)-2-hepten-4-yne

55. In CsCl type structure, the co-ordination number of Cs^+ and Cl^- respectively are:

- (A) 6, 6
- (B) 6, 8
- (C) 8, 8
- (D) 8, 6

56. Which one of the following reactions will not result in the formation of a

carbon-carbon bond?

- (A) Reimer-Tiemann reaction
- (B) Friedel Craft's acylation
- (C) Wurtz reaction
- (D) Cannizzaro reaction

57. Water is:

- (A) more polar than H_2S
- (B) more or less identical in polarity with H_2S
- (C) less polar than H_2S
- (D) None of these

58. Carboxylic acids are more acidic than phenol and alcohol because of:

- (A) intermolecular hydrogen bonding
- (B) formation of dimers
- (C) highly acidic hydrogen
- (D) resonance stabilization of their conjugate base

59. The order of increasing sizes of atomic radii among the elements O, S, Se, and As is:

(A) As < S < O < Se
(B) Se < S < As < O
(C) O < S < As < Se

(D) O < S < Se < As

60. Bauxite ore is generally contaminated with impurity of oxides of two elements X and Y. Which of the following statement is correct?

(A) X is a non-metal and belongs to the third period while Y is a metal and belongs to the fourth period.

- (B) One of two oxides has a three-dimensional polymeric structure.
- (C) Both (a) and (B) are correct.
- (D) None of the above.

61. The partial pressure of CH_3 OH(g), CO(g) and $H_2(g)$ in equilibrium mixture for the reaction,

$$CO(g) + 2H_2(g) \rightleftharpoons CH_3OH(g)$$

are 2.0, 1.0 and 0.1 atm respectively at $427^{\circ}C$. The value of K_p for the decomposition of CH_3OH to CO and H_2 is:

(A) 10^2 atm (B) 2×10^2 atm⁻¹ (C) 50 atm² (D) 5×10^{-3} atm²

62. The conjugate base of $(CH_3)_2NH_2^+$ is:

- $(A) (CH_3)_2 NH$
- $(B) (CH_3)_2 N^+$
- $(C) (CH_3)_3 N^+$
- (D) $(CH_3)_2N^-$

63. Which of the following is not present in a nucleotide?

- (A) Guanine
- (B) Cytosine
- (C) Adenine
- (D) Tyrosine

64. The shape of $[Cu(NH_3)_4]^{2+}$ is:

- (A) Tetrahedral
- (B) Square planar
- (C) Pyramidal
- (D) Octahedral

65. Heroin is a derivative of:

- (A) Cocaine
- (B) Morphine
- (C) Caffeine
- (D) Nicotine

66. The limiting equivalent conductivity of NaCl, KCl and KBr are 126.5, 150.0 and

151.5 S

 $cm^2 eq^{-1}$, respectively. The limiting equivalent ionic conductivity for Br is 78 S $cm^2 eq^{-1}$. The limiting equivalent ionic conductivity for Br is 78 S $cm^2 eq^{-1}$.

(A) 128
(B) 125
(C) 49
(D) 50

67. Rate of dehydration of alcohols follows the order:

(A) $2^{\circ} > 1^{\circ} > CH_3OH > 3^{\circ}$ (B) $3^{\circ} > 2^{\circ} > 1^{\circ} > CH_3OH$ (C) $2^{\circ} > 3^{\circ} > 1^{\circ} > CH_3OH$ (D) $CH_3OH > 1^{\circ} > 2^{\circ} > 3^{\circ}$

68. An alkene having molecular formula C_7H_{14} was subjected to ozonolysis in the presence of zinc dust. An equimolar amount of the following two compounds was obtained. The IUPAC name of the alkene is:

CH = O and =0

(A) 3,4-dimethyl-3-pentene

- (B) 3,4-dimethyl-2-pentene
- (C) 2,3-dimethyl-3-pentene
- (D) 2,3-dimethyl-2-pentene

69. Lanthanoid contraction can be observed in:

- (A) At
- (B) Gd
- (C) Ac
- (D) Lw

70. The form of iron obtained from blast furnace is:

- (A) Steel
- (B) Cast Iron
- (C) Pig Iron

Mathematics

71. A class has 175 students. The following data shows the number of students opting for one or more subjects. Maths = 100, Physics = 70, Chemistry = 40, Maths and Physics = 30, Maths and Chemistry = 28, Physics and Chemistry = 23, Maths, Physics,

and Chemistry = 18.

How many have offered Maths alone?

(A) 35

(B) 48

(C) 60

(D) 22

72. Let *R* be a relation on the set \mathbb{N} defined by

$$\{(x, y) \mid x, y \in \mathbb{N}, \, 2x + y = 41\}.$$

Then, R is:

(A) Reflexive

(B) Symmetric

(C) Transitive

(D) None of these

73. The function $f : \mathbb{R} \to \mathbb{R}$ defined by $f(x) = x^2 + x$ is:

(A) One-one

- (B) Onto
- (C) Many-one
- (D) None of these

74. If $12 \cot^2 \theta - 31 \csc \theta + 32 = 0$, then the value of $\sin \theta$ is:

(A) $\frac{3}{5}$ or 1

(B) $\frac{2}{3}$ or $-\frac{2}{3}$ (C) $\frac{4}{5}$ or $\frac{3}{4}$ (D) $\pm \frac{1}{2}$

75. The modulus of $(1 + i\sqrt{3})(2 + 2i) / (\sqrt{3} - i)$ is: (A) 2 (B) 4 (C) $3\sqrt{2}$

(D) $2\sqrt{2}$

76. If α, β are the roots of the equation $ax^2 + bx + c = 0$, then

$$\frac{\alpha}{a\beta+b} + \frac{\beta}{a\alpha+b} =$$

(A) $\frac{2}{a}$ (B) $\frac{2}{b}$ (C) $\frac{2}{c}$ (D) $-\frac{2}{a}$

77. The solution set of the inequality

 $37 - (3x + 5) \ge 9x - 8(x - 3)$ is:

(A) $(-\infty, 2)$ (B) $(-\infty, -2)$ (C) $(-\infty, 2]$ (D) $(-\infty, -2]$ **78. If** $\frac{n+2C8}{n-2P4} = \frac{57}{16}$, then the value of *n* is: (A) 20 (B) 19

(C) 18

79. The middle term in the expansion of

 $(10x + x^{10})^{10}$

is:

(A) 10C5

- **(B)** 10*C*6
- (**C**) 10*C*5*x*¹⁰

(D) 10*C*5*x*¹⁰

80. The fourth, seventh, and tenth terms of a G.P. are p, q, r respectively, then:

(A) $p^2 = q^2 + r^2$ (B) $q^2 = pr$ (C) $p^2 = qr$ (D) pqr + pq + 1 = 0

81. The point $(t^2 + 2t + 5, 2t^2 + t - 2)$ lies on the line x + y = 2 for:

(A) All real values of t

(B) Some real values of t

(C)
$$t = -3 \pm \frac{\sqrt{3}}{6}$$

(D) None of these

82. The equations of the lines which cut off an intercept 1 from the y-axis and are equally inclined to the axes are:

(A) x - y + 1 = 0, x + y + 1 = 0(B) x - y - 1 = 0, x + y - 1 = 0(C) x - y - 1 = 0, x + y + 1 = 0(D) None of these

83. The distance between the parallel lines

$$3x - 4y + 7 = 0$$
 and $3x - 4y + 5 = 0$ is $\frac{a}{b}$. Value of $a + b$ is:

(A) 2	
(B) 5	
(C) 7	
(D) 3	

84. For what value of k, does the equation

$$9x^2 + y^2 = k(x^2 - y^2 - 2x)$$

represent the equation of a circle?

(A) 1

(B) 2

(C) -1

(D) 4

85. A parabola has the origin as its focus and the line x = 2

as the directrix. Then the vertex of the parabola is at:

(A) (0, 2)

- **(B)** (1,0)
- $(\mathbf{C})(0,1)$
- $(\mathbf{D})(2,0)$

86. Equation of the ellipse whose axes are the axes of coordinates and which passes through the point (-3, 1) and has eccentricity $\sqrt{\frac{2}{5}}$ is:

(A) $5x^2 + 3y^2 - 48 = 0$ (B) $3x^2 + 5y^2 - 15 = 0$ (C) $5x^2 + 3y^2 - 32 = 0$ (D) $3x^2 + 5y^2 - 32 = 0$

87. The coordinates of the point which divides the line segment joining the points

(2, -1, 3) and (4, 3, 1) in the ratio 3 : 4 internally are: (A) $\left(\frac{2}{7}, \frac{20}{7}, \frac{10}{7}\right)$ (B) $\left(\frac{10}{7}, \frac{15}{7}, \frac{2}{7}\right)$ (C) $\left(\frac{20}{7}, \frac{5}{7}, \frac{15}{7}\right)$ (D) $\left(\frac{15}{7}, \frac{20}{7}, \frac{3}{7}\right)$

88. The relationship between *a* and *b* so that the function f(x) defined by

$$f(x) = \begin{cases} ax+1 & \text{if } x \le 3\\ bx+3 & \text{if } x > 3 \end{cases}$$

is continuous at x = 3, is:

(A) $a = b + \frac{2}{3}$ (B) $a - b = \frac{3}{2}$ (C) $a + b = \frac{2}{3}$ (D) a + b = 2

89. The function f(x) is given by:

$$f(x) = \begin{cases} x \sin\left(\frac{1}{x}\right) & \text{for } x \neq 0\\ 0 & \text{for } x = 0 \end{cases}$$

(A) continuous as well as differentiable

(B) differentiable but not continuous

(C) continuous but not differentiable

(D) neither continuous nor differentiable

90. The variance of the data 2, 4, 6, 8, 10 is:

(A) 8

(B) 7

- (C) 6
- (D) None of these

91. Find the probability of getting the sum as a perfect square number when two dice are thrown together.

(A) $\frac{5}{12}$

(B) $\frac{7}{18}$

(C) $\frac{7}{36}$ (D) None of these

92. The principal value of $\sin^{-1}\left(\sin\frac{5\pi}{3}\right)$ is:

(A) $-\frac{5\pi}{3}$ (B) $\frac{5\pi}{3}$ (C) $-\frac{\pi}{3}$ (D) $\frac{4\pi}{3}$

93. If the system of linear equations

$$x + ky + 3z = 0, \quad 3x + ky - 2z = 0, \quad 2x + 4y - 3z = 0$$

has a non-zero solution (x, y, z), then $\frac{xz}{y^2}$ is equal to:

(A) 10

- (B) -30
- (C) 30
- (D) -10

94. The value of the definite integral

$$\int_0^{\frac{\pi}{2}} \log(\tan x) \, dx \text{ is:}$$

(A) 0

- (B) $\frac{\pi}{4}$
- (C) $\frac{\pi}{2}$
- (D) *p*

95. The area enclosed between the graph of
$$y = x^3$$
 and the lines

$$x = 0, y = 1, y = 8$$
 is:

(A) $\frac{45}{4}$

(B) 14

(C) 7

96. The total number of 3-digit numbers, the sum of whose digits is even, is equal to:

(A) 450

(B) 350

- (C) 250
- (D) 325

97. To fill 12 vacancies, there are 25 candidates of which five are from the scheduled caste. If 3 of the vacancies are reserved for scheduled caste candidates while the rest are open to all, then the number of ways in which the selection can be made is:

- (A) $5C3 \times 22C9$
- **(B)** 22*C*9 5*C*3
- (C) 22C3 + 5C3
- (D) None of these

98. If

1	1	1
$\overline{q+r}$,	$\overline{r+p}$,	$\overline{p+q}$

are in A.P., then: (A) p, q, r are in A.P. (B) p^2, q^2, r^2 are in A.P. (C) $\frac{1}{p}, \frac{1}{q}, \frac{1}{r}$ are in A.P. (D) p + q + r are in A.P.

99. The sum of the first n terms of the series

$$1^2 + 2.2^2 + 3^2 + 2.4^2 + 5^2 + 2.6^2 + \cdots$$

is

(A)

$$\frac{n(n+1)^2}{2} \text{ when n is even. When n is odd the sum is}$$
 (A) $\left[\frac{n(n+1)}{2}\right]^2$ (B) $\frac{n^2(n+1)}{2}$

(C) $\frac{n(n+1)^2}{4}$ (D) $\frac{3n(n+1)}{2}$

100. The locus of a point that is equidistant from the lines

 $x + y - 2\sqrt{2} = 0$ and $x + y - \sqrt{2} = 0$ is:

(A) $x + y - 5\sqrt{2} = 0$ (B) $x + y - 3\sqrt{2} = 0$ (C) $2x + 2y - 3\sqrt{2} = 0$ (D) $2x + 2y - 5\sqrt{2} = 0$

101. The point diametrically opposite to the point P(1,0) on the circle

$$x^{2} + y^{2} + 2x + 4y - 3 = 0$$
 is:

- (A) (3, -4)
- **(B)** (−3, 4)
- (C) (-3, -4)
- (D)(3,4)

102. For the parabola $y^2 = -12x$, the equation of the directrix is x = a. The value of a

is:

(A) 3 (B) 4

- (C) 2
- (D) 6

103. The eccentricity of the curve

$$2x^2 + y^2 - 8x - 2y + 1 = 0$$
 is:

(A) $\frac{1}{2}$ (B) $\frac{1}{\sqrt{2}}$ (C) $\frac{2}{3}$ **104.** The equation of the hyperbola with vertices at $(0, \pm 6)$ and $e = \frac{5}{3}$ is:

(A) $\frac{x^2}{36} - \frac{y^2}{64} = 1$ (B) $\frac{y^2}{36} - \frac{x^2}{64} = 1$ (C) $\frac{x^2}{64} - \frac{y^2}{36} = 1$ (D) $\frac{y^2}{64} - \frac{x^2}{36} = 1$

105. The following determinant is equal to:

$\sin^2 x$	$\cos^2 x$	1
$\cos^2 x$	$\sin^2 x$	1
-10	12	2

(A) 0

- (B) $12\cos^2 x 10\sin^2 x$
- (C) $12\cos^2 x 10\sin^2 x 2$

(**D**) 10 sin 2*x*

107. The local minimum value of the function

$$f(x) = 3 + |x|, \quad x \in \mathbb{R}$$

is:

(A) 1

(B) 2

(C) 3

(D) 0

108. The value of the integral

$$\int_0^{\frac{\pi}{2}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} \, dx$$

is:

(A) $\frac{\pi}{2}$

(B) $-\frac{\pi}{2}$ (C) $\frac{\pi}{4}$ (D) None of these

109. The equation of the plane which bisects the angle between the planes

3x - 6y + 2z + 5 = 0 and 4x - 12y + 3z - 3 = 0 which contains the origin is:

- (A) 33x 13y + 32z + 45 = 0(B) x - 3y + z - 5 = 0(C) 33x + 13y + 32z + 45 = 0
- (D) None of these

110. An urn contains five balls. Two balls are drawn and found to be white. The probability that all the balls are white is:

(A) $\frac{1}{10}$ (B) $\frac{3}{10}$ (C) $\frac{3}{5}$ (D) $\frac{1}{2}$

Aptitude

111. What is the total marks obtained by Meera in all the subjects?

- (A) 448
- (B) 580
- (C) 470
- (D) 74.67

112. What is the average marks obtained by these seven students in History? (rounded off to two digits)

- (A) 72.86
- (B) 27.32

(C) 24.86

(D) 29.14

113. How many students have got 60% or more marks in all the subjects?

(A) One

(B) Two

(C) Three

(D) Four

114. A series is given, with one term missing. Choose the correct alternative from the given ones that will complete the series.

5, 11, 24, 51, 106, _?

(A) 122

(B) 217

(C) 120

(D) 153

115. In a certain code, BANKER is written as LFSCBO. How will CONFER be written in that code?
(A) GFSDPO
(B) GFSEPO
(C) FGSDOP
(D) FHSDPO

116. Kailash faces towards north. Turnings to his right, he walks 25 metres. He then turns to his left and walks 30 metres. Next, he moves 25 metres to his right. He then turns to the right again and walks 55 metres. Finally, he turns to the right and moves 40 metres. In which direction is he now from his starting point?

(A) South-West

(B) North-West

(C) South

117. An accurate clock shows 8 O'clock in the morning. Through how many degrees will the hour hand rotate when the clock shows 20:00 (8 O'clock in the evening)?

(A) 144°

(B) 150°

(C) 168°

(D) 180°

118. Two statements are given followed by three conclusions numbered I, II, and III. Assuming the statements to be true, even if they seem to be at variance with commonly known facts, decide which of the conclusions logically follow(s) from the statements.

Statements: 1. All utensils are spoons. 2. All bowls are spoons.

Conclusions: I. No utensil is a bowl. II. Some utensils are bowls. III. No spoon is a utensil.

(A) Only conclusion I follows

(B) Conclusions I and III follow

(C) Either conclusion I or II follows

(D) Only conclusion III follows

119. What was the ratio between the ages of P and Q four years ago? I. The ratio between the present ages of P and Q is 3 : 4. II. The ratio between the present ages of Q and R is 4 : 5.

(A) if the data in statement I alone is sufficient to answer the question, while the data in statement II alone is not sufficient to answer the question.

(B) if the data in statement II alone is sufficient to answer the question, while the data in statement I alone is not sufficient to answer the question.

(C) if the data in both the statements I and II together are not sufficient to answer the question.

(D) if the data in both the statements I and II together are necessary to answer the question.

120. What was the cost price of the suitcase purchased by Samir? I. Samir got a 25

percent concession on the labelled price. II. Samir sold the suitcase for ₹2000 with 25 percent profit on the labelled price.

(A) if the data in statement I alone is sufficient to answer the question, while the data in statement II alone is not sufficient to answer the question.

(B) if the data in statement II alone is sufficient to answer the question, while the data in statement I alone is not sufficient to answer the question.

(C) if the data in both the statements I and II together are not sufficient to answer the question.

(D) if the data in both the statements I and II together are necessary to answer the question.

English

121. Read the following passage and answer the question that follows.

"His instrument struck against something hard, dangerously near the kidney.... 'It is not quite at the kidney, my friend,' Sadao murmured.... 'My friend,' he always called his patients and so he did now, forgetting that this was his enemy."

To whom does Sadao attend to in the lines above?

- (A) A relative
- (B) His friend
- (C) His enemy
- (D) A patient

122. Choose the correct pronunciation for the word 'sorbet' from the following options:

- (A) sore-bet
- (B) sore-bay
- (C) sore-bye
- (D) shore-bay

123. What is the correct syllable division of the word 'indomitable'?

- (A) in do mit able
- (B) in dom i ta ble

(C) in - do - mi - ta - ble(D) in - dom - i - table

124. Read the following passage and the question below. Choose the correct answer.

Gandhi never contented himself with large political or economic solutions. He saw the cultural and social backwardness in the Champaran villages and wanted to do something about it immediately. He appealed to teachers.

Which of the following statements is true about the passage?

- (A) Gandhi was dissatisfied with political or economic solutions
- (B) Gandhi was interested in the welfare of teachers of Champaran villages
- (C) Gandhi was happy about the cultural and social backwardness of Champaran villages
- (D) Gandhi was hopeful that teachers could save villages from cultural and social

backwardness

125. Choose the correct meaning of the idiom 'a bolt out of the blue' from the given options:

- (A) Something totally unexpected
- (B) Lightning and thunderstorm
- (C) To do something kind
- (D) To mourn after someone